## Unit 3 <br> Equations of Lines <br> Lesson Outline

## BIG PICTURE

Students will:

- Manipulate and solve algebraic equations, to solve problems;
- Graph a line and write the equation of a line from given information.

| Day | Lesson Title | Math Learning Goals | Expectations |
| :---: | :---: | :---: | :---: |
| 1 | Reminiscing Old Relationships | - Activate prior knowledge from grade 9 Applied on Linear Relations <br> - Collect data, create a scatter plot and line of best fit <br> - Make connections in context for initial value and the rate of change of a linear relation | ML2.01 <br> CGE 3b, 5a |
| 2 | Why Mr Y depends on Ms X? | - Identify that $\mathrm{y}=\mathrm{mx}+\mathrm{b}$ is a common form for the equation of a line. <br> - Make connections between the initial value and the rate of change in the relation to the $y$-intercept and slope of the equation of the line <br> - Identify the geometric significance of $m$ and $b$ in the equation $y=$ $m x+b$. <br> - Write linear equations for relationships in context, e.g., an electrician charges $\$ 65$ as a base fee and $\$ 35$ for each hour. <br> - Given a linear equation in slope y-intercept form, write a story in context. | $\begin{aligned} & \hline \text { ML2.01 } \\ & \text { ML2.02 } \\ & \text { ML2.03 } \\ & \text { CGE 4f } \end{aligned}$ |
| 3 | Slopes and Stuff | - Investigate the properties of the slopes of lines segments, using graphing calculators. <br> - Investigate the steepness of lines, from their graphs. <br> - Identify similarities and differences between lines with positive and negative slopes and parallel lines. <br> - Using GSP ${ }^{\circledR} 4$ and the plot points feature to find slopes of various lines to determine their characteristics. | $\begin{aligned} & \text { ML2.03 } \\ & \text { ML2.04 } \\ & \text { CGE 5b, 5a } \end{aligned}$ |
| 4 | Can Graphing Get Any Easier? | - Graph lines by hand using the y-intercept and slope given the equation in the slope $y$-intercept form | $\begin{aligned} & \text { ML2.05 } \\ & \text { ML2.06 } \\ & \text { CGE 5b, 7b } \end{aligned}$ |
| 5 | Temperature Conversions | - Determine a linear equation to convert between Celsius and Fahrenheit temperature <br> - Solve one variable equations with fractional coefficients in context using CAS and pencil and paper. | $\begin{aligned} & \text { ML1.01 } \\ & \text { ML1.02 } \end{aligned}$ |


| Day | Lesson Title | Math Learning Goals | Expectations |
| :---: | :---: | :---: | :---: |
| 6 | Can You Stop the Fire? | - Create a scatter plot and line of best fit from collected data. <br> - Determine the equation of the line of best fit by hand. <br> - Verify the scatter plot and equation of line of best fit using technology <br> - Write linear equations for relationships in context from given information. <br> - Create contexts for given linear relations in slope y-intercept form. | ML2.01, ML2.02, <br> ML2.03, ML2.04, ML2.06 <br> CGE 3c, 4b |
| 7. | Y the X Are You Intercepting Me? | - Determine the x and y intercepts of a linear relation. <br> - Determine the x and y intercepts of a linear relation in standard form. <br> - Graph lines in standard form by hand using the x and y intercepts. <br> - Solve linear equations involving one variable. | $\begin{aligned} & \text { ML1.03 } \\ & \text { ML2.05 } \end{aligned}$ |
| 8. | Slopes Away | - Determine the equation of a line, given the slope and y-intercept <br> - Given two points, write the equation of a line. <br> - Determine the slope of the line using rate triangles and the formula. | ML1.01 <br> ML1.03 <br> ML2.05 <br> ML2.06 <br> CGE 5b |
| 9 | Yes, we Have No Graph Paper | - Write the equation of a line given a point and a slope or two points <br> - Write linear equations for relationships in context. | $\begin{aligned} & \text { ML1.01 } \\ & \text { ML2.06 } \\ & \text { CGE 5b } \end{aligned}$ |
| 10. | So, You Think You Know Everything About Lines? | - Review x- and y-intercepts. <br> - Investigate the special cases $\mathrm{x}=\mathrm{a}$ and $\mathrm{y}=\mathrm{b}$. <br> - Express the equation of a line in the form $y=m x+b$, given the form $\mathrm{Ax}+\mathrm{By}+\mathrm{C}=0$. | ML1.03 <br> ML2.02 <br> ML2.05 <br> CGE, 5a, 5e |
| 11 | London Bridge is Falling Down | - Collect data on linear relations in context of real-life problems <br> - Determine the equation of the linear relation <br> - Relate the slope and intercepts in the context of real-life applications <br> Note: This lesson could also be used as a summative performance task. | ML1.01- ML1.03 <br> ML2.01- ML2.06 <br> CGE 5b |
| 12 | Summative <br> Assessment | Sample unit review questions provided. <br> Note: A summative performance task is available from the members only section of the OAME web site www.oame.on.ca | $\begin{aligned} & \text { MLV. } 001 \\ & \text { MLV. } 002 \end{aligned}$ |
| 13 | Jazz Day |  |  |



### 3.1.1 Definition Match

## Definitions:

|  | An orderly arrangement of facts set out for easy reference (e.g., <br> an arrangement of numerical values in vertical and horizontal <br> columns) |
| :--- | :--- |
|  | The difference between two consecutive y-values in a table in <br> which the difference between the x-values is constant |
|  | The vertical distance between two points |
|  | A relation in which the graph forms a straight line |
|  | A relation in which one variable is a multiple of the other between two points |
|  | A relation in which one variable is a multiple of the other plus a <br> constant amount |
|  | A description of how two variables are connected |
| The change in one variable relative to the change in another |  |
|  | In a relation, the variable whose values you calculate; usually <br> placed in the left column in a table and on the vertical axis in a <br> graph |
|  |  |

### 3.1.1 Definition Match (continued)

|  | In a relation, the variable whose values you choose; usually <br> placed in the right column in a table of values and on the <br> horizontal in a graph |
| :--- | :--- |
|  | A line that best describes the relationship between two variables <br> in a scatter plot |
|  | A symbol used to represent an unspecified number. For <br> example, $x$ and $y$ are variables in the expression $x+2 y$ |
|  | A relation whose graph is not a straight line |

## Graph:


$=$ $\qquad$

### 3.1.1 Definition Match (continued)

## Equation

|  | $=$ | $x$ |
| :--- | :--- | :---: |
| OR |  |  |
|  | $=$ | + |
|  |  |  |
|  |  |  |

## Table of Values



### 3.1.2: Definition Match - Teacher

Below are the values needed to fill the chart and blanks for the activity above. Make sufficient copies for every student. Cut these out, mix them up and place these into an envelope:

| Dependent Variable | Dependent Variable | Dependent Variable | Dependent Variable |
| :---: | :---: | :---: | :---: |
| Dependent Variable | Direct Variation | First Differences | First Differences |
| Independent Variable | Independent Variable | Independent Variable | Independent Variable |
| Independent Variable | Initial Value | Initial Value | Initial Value |
| Initial Value | Initial Value | Line of Best Fit | Linear Relation |
| Non-linear Relation | Partial Variation | Rate of Change | Rate of Change |
| Rate of Change | Rate of Change | Rate of Change | Relation |
| Rise | Rise | Rise | Rise |
| Rise | Run | Run | Run |
| Run | Run | Table of Values | Variable |

### 3.1.3 Definition Match - Solution

## Definitions:

| Table of Values | An orderly arrangement of facts set out for easy reference (e.g., <br> an arrangement of numerical values in vertical and horizontal <br> columns) |
| :--- | :--- |
| First Differences | The difference between two consecutive y-values in a table in <br> which the difference between the x-values is constant |
| Rise | The vertical distance between two points |
| Run horizontal distance between two points |  |
| Linear Relation | A relation in which the graph forms a straight line |
| Direct Variation | A relation in which one variable is a multiple of the other |

### 3.1.1 Definition Match - Solution (Continued)

| Dependent Variable | In a relation, the variable whose values you choose; usually <br> placed in the right column in a table of values and on the <br> horizontal in a graph |
| :--- | :--- |
| Line of Best Fit | A line that best describes the relationship between two variables <br> in a scatter plot |
| Variable | A symbol used to represent an unspecified number. For <br> example, $x$ and $y$ are variables in the expression $x+2 y$ |
| Non-Linear Relation | A relation whose graph is not a straight line |



### 3.1.1 Definition Match - Solution (Continued)

## Equation



### 3.1.4: Reminiscing Old Relationships

There are 4 different envelopes that match the relationships below. Partner A will work on ENVELOPES A and C, Partner B will work on ENVELOPES B and D. Your job is to glue the appropriate values from your envelope onto the space provided.


| ENVELOPE B |  |
| :---: | :---: |
| Money, Money! <br> Ayda receives a base salary of $\$ 200$ and $\$ 50$ for every audio system he sells. | Internet Fees <br> An internet package charges a flat fee of $\$ 10$ plus $\$ 0.40$ per hour. |
| Initial Value: | Initial Value: |
| Rate: | Rate: |
| Independent Variable: | Independent Variable: |
| Dependent Variable: | Dependent Variable: |

### 3.1.4: Reminiscing Old Relationships (Continued)



### 3.1.4: Reminiscing Old Relationships (Continued)



### 3.1.5: Reminiscing Old Relationships - Teacher

Below are the values needed to fill the charts for the activity above. Cut these out, mix them up and place these into separate envelopes:

Note: Paste the envelope name on the outside of the envelope
$\mathscr{H}$
ENVELOPE A

| 300 | 0 |
| :---: | :---: |
| 20 | 10 |
| Number of People | Time |
| Cost | Earnings |

$\mathscr{H}$
ENVELOPE B

| 200 | 10 |
| :---: | :---: |
| 50 | 0.40 |
| Number of Audio Systems | Time |
| Earnings | Cost |

### 3.1.5: Reminiscing Old Relationships -Teacher (Continued)

Below are the values needed to fill the charts for the activity above. Cut these out, mix them up and place these into separate envelopes:
$\leftrightarrow$
ENVELOPE C

| 0 | 100 |
| :---: | :---: |
| 2 | 1 |
| Distance | Cost |
| Time | Distance |

$\mathscr{H}$
ENVELOPE D

| 10 | 10 |
| :---: | :---: |
| 2 | 20 |
| Cost | Cost |
| Time | Time (Days) |

### 3.1.6: A Mathematical Spelling Bee

## Procedure

1. You will work in partners where Partner $A$ is the timer and Partner $B$ is the recorder.
2. Create four quadrants by folding a piece a paper in half and fold in half again.
3. With a watch, student A will signal student $B$ to start printing the full word RUN down one of the paper quarters as many times possible in 10 seconds. This is not a contest print at your normal printing speed.
4. After 10 seconds, student $B$ signals student $A$ to stop printing.
5. Count all the legible words.
6. Record this value in the table below.
7. Repeat steps 1 - 6 for the words RATE, VALUE, CHANGE and INITIAL

## Recording Data

8. Record this value in the table below.

| Word | Word Length | Number of Words Written |
| :---: | :--- | :--- |
| RUN |  |  |
| RATE |  |  |
| VALUE |  |  |
| CHANGE |  |  |
| INITIAL |  |  |

9. What is the independent variable? $\qquad$
10. What is the dependent variable? $\qquad$

### 3.1.6: A Mathematical Spelling Bee (Continued)

11. Create a scatter plot from your data on the grid provided. Label the axis with the independent variable on the x-axis and dependent variable on the $y$-axis.

12. Draw a line of best fit from the scatter plot above. Extend your line to both the $x$-axis and $y$ axis.
13. Using a rate triangle, calculate the rate of change of your line of best fit. $\qquad$
14. Interpret the meaning of the rate of change as it relates to this activity.
15. At what value does the line cross the $y$-axis? $\qquad$
16. Interpret this value in the context of this activity.
17. At what value does the line cross the $x$-axis?? $\qquad$
18. Interpret this value in the context of this activity.

### 3.1.7: Linear Relation Concept Map - Teacher



### 3.1.8: Variables and Equations with Graphs

For each of the following graphs determine:
a) The rate and the initial value from the graph. Show your work on the graph.
b) A rule in words that relates the balance (B), the number ( $n$ ) of weekly withdrawals or deposits and the initial amount in the account; and
c) An algebraic rule relating Balance (B), the number of weekly withdrawals/deposits (n) and the initial value in the account
d) Determine how much will be in the account after 12 weeks using the formula.

1. This person is withdrawing/depositing that is positive/negative correlation. Circle correct answers.

b) Rule in words:

Balance starts at $\qquad$ and
$\qquad$ (increase/decrease)by
$\qquad$ per week(rate).

## c) Algebraic Rule

$B=$
d) After 12 weeks
2. This person is withdrawing/depositing that is positive/negative correlation. Circle correct answers.

b) Rule in words:

Balance starts at $\qquad$ and
$\qquad$ (increase/decrease)by
$\qquad$ per week(rate).

## c) Algebraic Rule

$B=$
d) After 12 weeks.

### 3.1.8: Variables and Equations with Graphs (Continued)

3. This person is withdrawing/depositing that is positive/negative correlation. Circle correct answers.

b) Rule in words:

Balance starts at $\qquad$ and
$\qquad$ (increase/decrease)by ___ per week(rate).

## c) Algebraic Rule

$B=$
d) After 12 weeks.

On a graph, the initial value is shown as the $\qquad$
On a graph, the rate is shown as $\qquad$
4. This person is withdrawing/depositing that is positive/negative correlation. Circle correct answers.

b) Rule in words:

Balance starts at $\qquad$ and
$\qquad$ (increase/decrease)by
$\qquad$ per week(rate).

## c) Algebraic Rule

$B=$
d) After 12 weeks.

### 3.1.8: Variables and Equations with Graphs (Continued)

5. This person is withdrawing/depositing that is positive/negative correlation. Circle correct answers.

b) Rule in words:

Balance starts at $\qquad$ and
$\qquad$ by $\qquad$ per week.

## c) Algebraic Rule

$B=$
d) After 12 weeks.
6. This person is withdrawing/depositing that is positive/negative correlation. Circle correct answers.

b) Rule in words:

Balance starts at $\qquad$ and
$\qquad$ by $\qquad$ per week.

## c) Algebraic Rule

$B=$
d) After 12 weeks.


### 3.2.1: Agree to Disagree

For each question stand if you agree or remain sitting if you
disagree.

a) Point A has coordinates $(3,-2)$
b) Point $B$ has coordinates $(3,4)$
c) Point C has coordinates $(-1,1)$
d) Point $A$ is in Quadrant 4
e) The origin is located at $(0,0)$

a) The rate of change is $\$ 25 /$ week
b) The initial value is $\mathbf{\$ 2 0 0}$

Class Consensus (Agree / Disagree)
a)
b)
c)
d)
e)
)
a)
b)

### 3.2.1: Agree to Disagree (Continued)

For each question stand if you agree or remain sitting if you
disagree.

Class Consensus (Agree / Disagree)

A family meal deal at Chicken Deluxe costs $\$ 26$, plus $\$ 1.50$ for every extra piece of chicken added to the bucket.
a) The rate of change is $\$ 26$.
b) The initial value is $\mathbf{4 2 6}$.
c) The independent variable is number of pieces of chicken

A Chinese food restaurant has a special price for groups. Dinner for two costs $\$ 24$ plus $\$ 11$ for each additional person.
a) The rate of change is $\$ 11$
b) The initial value is $\mathbf{\$ 1 1}$
c) The dependent variable is the number of people

| Number of <br> Toppings |  |
| :--- | :--- |
| 0 | Cost of a <br> Large Pizza <br> (\$) |
| 1 | 9.40 |
| 2 | 11.50 |
| 3 | 13.60 |
| 4 | 15.70 |

a) The initial value is $\mathbf{9 . 4 0}$
b) The rate of change is $\mathbf{\$ 1 . 1 0}$
c) Dependent variable is the Cost of a Large Pizza
a)
b)
c)
a)
b)
c)
a)

b)
c)

c) Dependent variable is the Cost of a Large Pizza

### 3.2.2: Exploring an MB Eh!

$$
\begin{aligned}
& \text { Y-int Slope Form } \\
& \qquad y=m x+b
\end{aligned}
$$

What does the m and b represent?

## Exploring the $m$

- We already know that in a table of values for a linear relationship a pattern will form. This pattern is the
- Pattern $\rightarrow$

| $X$ | $Y$ |
| :---: | :---: |
| -2 | 4 |
| -1 | 6 |
| 0 | 8 |
| 1 | 10 |
| 2 | 12 |

Equation $\rightarrow$

### 3.2.2: Exploring an MB Eh! (Continued)

## Exploring the $m$

- What is the pattern?
- Pattern $\rightarrow$
- What is the equation?

| $X$ | $Y$ |
| :---: | :---: |
| -2 | 7 |
| -1 | 4 |
| 0 | 1 |
| 1 | -2 |
| 2 | -5 |

## Equation $\rightarrow$

## Exploring the $m$

- What is the slope?



### 3.2.2: Exploring an MB Eh! (Continued)



### 3.2.2: Exploring an MB Eh! (Continued)

## What does the $m$ represent?

> What is the slope and what does the $m$ represent?
> $y=\frac{3}{2} x$
> $y=\frac{1}{5} x$
> $y=\frac{-5}{2} x$

### 3.2.2: Exploring an MB Eh! (Continued)

## Exploring the b

- Look at the table and look at the equation.
-What do you notice?
- When $\mathrm{x}=0 \rightarrow$
- Equation has

| $X$ | $Y$ |
| :---: | :---: |
| -2 | 4 |
| -1 | 6 |
| 0 | 8 |
| 1 | 10 |
| 2 | 12 |

## Equation $\rightarrow$

## Exploring the $b$

- Look at the table and look at the equation.
-What do you notice?
- When $\mathrm{x}=0 \rightarrow$
- Equation has

| $X$ | $Y$ |
| :---: | :---: |
| -2 | 7 |
| -1 | 4 |
| 0 | 1 |
| 1 | -2 |
| 2 | -5 |

Equation $\rightarrow$

### 3.2.2: Exploring an MB Eh! (Continued)

## Exploring the b

- What is the slope?


What does the b represent?

### 3.2.2: Exploring an MB Eh! (Continued)

## What does the equation tell you?

- $y=4 x-1$
- $y=3 / 2 x+2$
- $y=1 / 5 x-3$
- $y=-2 x$
- $y=-5 / 2 x+10$


### 3.2.3: Presentation Y-int Slope Form

## Y-int Slope Form.ppt



1


3


What does the $m$ represent?

- The $m$ represents the slope of the line.
- Describes how steep the line is
- The numerator tells us to go up or down (RISE)
- The denominator tells us to go RIGHT (RUN)
- If the numerator is positive we go up
- If the numerator is negative we go down
- Tells you the pattern in a table of values


Exploring the $m$

- What is the slope?


What is the slope and what does the $m$ represent?
$y=\frac{3}{2} x$
$y=\frac{1}{5} x$
$y=\frac{-5}{2} x$

8

### 3.2.3: Presentation Y-int Slope Form (Continued)



9


What does the equation tell you?

- $y=4 x-1$
- $y=3 / 2 x+2$
- $y=1 / 5 x-3$
- $y=-2 x$
- $y=-5 / 2 x+10$


## Exploring the $b$

- Look at the table and look at the equation.
-What do you notice?
- When $x=0 \rightarrow y=1$
- Equation has + 1

| $X$ | $Y$ |
| :---: | :---: |
| -2 | 7 |
| -1 | 4 |
| 0 | 1 |
| 1 | -2 |
| 2 | -5 |

$$
\text { Equation } \rightarrow y=-3 x+1
$$

10

What does the b represent?

- It is the $y$-intercept (where it crosses the $y$ axis)
- The value when $\mathrm{x}=0$

12

### 3.2.4: Why Mr. Y depends on the independent Ms. X?

Complete the tables on the next two pages that compare and contrast terms, equations, tables of values and graphs between grade 9 and grade 10.

|  | New Grade 10 <br> Topics - y- <br> intercepts, slope, $x$ <br> and $y$ | Similarities | Differences |
| :---: | :---: | :---: | :---: |
| Terminology |  |  |  |
|  |  |  |  |
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|  |  |  |  |
| Equation |  |  |  |
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|  |  |  |  |

### 3.2.4: Why Mr. Y depends on the independent Ms. X? (Continued)

| Grade 9 Topics - <br> Initial Value, Rate of <br> Change, Independent <br> and Dependent <br> Variable | New Grade 10 <br> Topics $-\mathbf{y -}$ <br> intercepts, slope, $x$ <br> and $\mathbf{y}$ | Similarities |  |
| :--- | :--- | :--- | :--- |
| Table of Values |  |  | Differences |
|  |  |  |  |

### 3.2.4: Why Mr. Y depends on the independent Ms. X? (Continued)

Complete the following table for each equation given. Provide a different context for each row if possible.

| Equation | Slope | Real Context for Slope | y-intercept | $\begin{aligned} & \text { Real context } \\ & \text { for } y \text { - } \\ & \text { intercept } \\ & \hline \end{aligned}$ | Real context equation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $Y=2.5 x+5$ | 2.5 | \$2.50/km | 5 | \$5 starting fee | $C=\$ 2.50 \mathrm{~d}+\$ 5$ <br> (C represents cost and d represents distance a cab travels) |
| $Y=2 x+17$ |  |  |  |  |  |
| $y=250-10 x$ |  |  |  |  |  |
| $y=1.5+x$ |  |  |  |  |  |
| $y=100 x-2000$ |  |  |  |  |  |
| $y=75 x$ |  |  |  |  |  |


| Unit 3 Day 3: Slopes and Stuff |  | Grade 10 <br> Applied |
| :---: | :---: | :---: |
| Minds On: 5 Min. | Math Learning Goals <br> Students will: <br> - Investigate the properties of the slopes of lines segments, using graphing calculators. <br> - Investigate the steepness of lines, from their graphs. <br> - Identify similarities and differences between lines with positive and negative slopes and parallel lines. <br> - Using GSP ${ }^{\circledR} 4$ and the plot points feature to find slopes of various lines to determine their characteristics. | Materials <br> - BLM 3.3.1 3.3.8 <br> - Graphing calculators <br> - Computers with $\mathrm{GSP}^{\circledR} 4$ <br> - Scissors |
| Action: 60 Min |  |  |
| Consolidate/ Debrief: 10 Min |  |  |
| Assessment Opportunities |  |  |
|  |  |  |  |  |
| Minds On... | Pair $\rightarrow$ Pair/Share <br> Assign heterogeneous pairs. <br> Partner A: tells Partner B what a slope is. <br> Partner B: tells Partner A what y-intercept is. <br> Together: please make up an equation in the $y=m x+b$ form <br> Whole Class $\rightarrow$ Discussion <br> Discuss and review what slope and $y$-intercept is and review $y=m x+b$ |  |
| Action! | Individual $\rightarrow$ Transfrm Tutorial <br> Cut out equations from BLM 3.3.3 and randomly distribute to each student. Distribute graphing calculators to students. Students follow instructions on BLM 3.3.1 and complete the first 10 questions on BLM 3.3.2 <br> Whole Class $\rightarrow$ Parallel Lines Investigation <br> Students continue from page 3 on BLM 3.3.2 and, using the graphing calculator to verify, they will find other students whose lines are parallel. | Refer to BLM 3.3.7 for the teacher instructions on using Transfrm application for TI-83+/TI-84. <br> If graphing calculators are not available, instructions have been written and |
| Consolidate Debrief | Whole Class $\rightarrow$ Guided Discussion <br> Encourage pairs whose lines are parallel to identify themselves and sharing their equations with the group. <br> Lead a discussion concluding the conditions for lines to be parallel. | included for GSP®4. <br> Note: Students worksheets/activities are different than the worksheets for TI- <br> 83. Check BLM 3.3.8 for teacher instructions and BLM 3.3.5 for students. |
| Application Concept Practice | Home Activity or Further Classroom Consolidation <br> Students complete BLM 3.3.6. Students name the slopes (AB, BC, etc.), indicate whether it is a positive or negative slope and find parallel slopes (if any). |  |

### 3.3.1 Slopes and Stuff on TI-83

## Instructions for TI-83

Ok, if you follow this step-by-step, it will be fool-proof. Let's start!

## Press ON

Press APPS
Scroll and find TRANSFRM
Press ENTER

## Select UNINSTALL by pressing ENTER

Press APPS again
Scroll and find TRANSFRM
Press ENTER
Now the screen should say "PRESS ANY KEY", so press any key to continue
Your screen will say DONE
Press $\mathrm{Y}=$ (grey button, white font, top left)
You now need to enter $\mathbf{A X}+\mathbf{B}$.
Do you see all the green letters on the calculator? You can get to them by pressing the ALPHA button (green button, white font)
So, to get A, you need to press ALPHA, then MATH. See?
X is the button to the right of the ALPHA button (the button with $\mathbf{X}, \mathbf{T},, \mathbf{n}$ )
The " + " sign you can find for sure and can you figure out how to type $B$ ?
So now you should have $A X+B$ entered on the screen!
A few more steps and we're ready to graph.
Press WINDOWS
Scroll up once so that SETTINGS is highlighted
Scroll down and change $A$ to 1 , change $B$ to 1 and change Step to 1 .
Ok, you're ready!

## Press GRAPH!

Scroll right and left to see what happens to A.
If you want to play with $B$, scroll down once so that the equal sign for $B$ is highlighted and then scroll right and left as well to change $B$.

### 3.3.2 Slopes and Stuff on TI-83 Investigation

## Worksheet for graphing calculator

| 1. Describe the graph when $A$ is greater <br> than 1. | Draw an example. |
| :--- | :--- |
| 2. What is the difference between $A=2$ <br> and $A=6$ ? | Draw $A=2$ on the left and draw $A=6$ on <br> the right. |
| 3. What happens when $A=0$ ? | Draw an example. |

### 3.3.2 Slopes and Stuff on TI-83 Investigation (continued)

6. When you are changing $A$, what stayed the same?

| 7. What happens when $\mathrm{B}=5$ ? | Draw an example. |
| :--- | :--- |
| 8. What happens when $\mathrm{B}=-6$ ? | Draw an example. |

9. When you are changing $B$, what stayed the same?
10. In the equation $y=m x+b$, what does letter $A$ represent? What about $B$ ?

### 3.3.2 Slopes and Stuff on TI-83 Investigation (continued)

Almost done. But since we're finished with the Transform applications, please help me uninstall it first before we move on.

## Press APPS

Scroll and find TRANSFRM
Press ENTER
Select UNINSTALL by pressing ENTER
Using your equation that you got from your teacher, type this into your graphing calculator.
Press $\mathbf{Y}=$ and enter the equations (remember, X is the button with $\mathbf{X}, \mathbf{T}$, , $\mathbf{n}$ ).
Press GRAPH
You should see your graph on your screen. Walk around the room and find a line that looks parallel to yours from another student. If you want to see whether the lines are parallel, type the equation from the student you found into your calculator as well. Just repeat the above instructions and enter the second equation into $\mathbf{Y}_{2}=$. Press GRAPH again.

Are they similar? If they are, compare the two equations. What is the same?
What can you conclude about parallel lines?
Check this by finding another pair of students and discuss your conclusions briefly with them.
Write down your conclusion below.


### 3.3.4 Slopes and Stuff on GSP- Optional Investigation

## Student Instructions for GSP

Ok, Geometer's Sketchpad is a great way to see just how the slope and y-intercepts work. Follow these instructions and they will help you create what you need in order for you to start investigating. Good luck!

THE GEOMEIER's SKETCHPAD'

First, let's launch Geometer's Sketchpad on the computer. Click on any white space to get rid of the logo.

Let's see some grid. Select Show Grid from the Graph menu. Great, now we're ready to create a line.

Select Plot Points from the Graph menu.
Enter 0 (left text box), and 1 (right text box).
Click Plot. Click Done.
Click on the Point Tool on the left hand side menu.
Create a point anywhere you want.
Click and hold the Line Tool on the left hand side menu until a line with arrows on both ends appear and select that option. Click on point $(0,1)$ and click on the point that you created to create a line.

Click on the Arrow Tool on the left hand side menu and click on any white space. Now click on the line so that only the line is highlighted.

Select Slope from the Measure menu. Click on any white space. Click on the line. If you point your cursor on Point B, you can now click and drag the line! Look at the slope number!

Answer questions 1-6 on the worksheet. ©
Now that you have looked at the slope, let's look at the y-intercept.
Select New Sketch from the File menu. Let's show some grid first (see instructions above).
Now, click on the Point Tool on the left hand side and create a point anywhere on the y-axis. Select Translate from the Transform menu. On the pop-up menu, click on Rectangular on the top. Enter 3 for Horizontal and 2 for Vertical (or any one-digit number that you want). Click Translate.

Select the Arrow Tool on the left hand side menu and click on any white space. Click on the point on the y-axis to highlight it and select Ordinate (y) from the Measure menu. Click on any white space.

### 3.3.4 Slopes and Stuff on GSP - Optional Investigation (continued)

Create a line with those two points (see instructions above). After you have created the line, click on any white space and then highlight the line. Select Slope from the Measure menu. Click on any white space and then highlight the line again.

Now as you move the line, look at the y-ordinate number and look at the slope value.
Answer questions $7-10$ on the worksheet. ©
Ok, a little bit more and the activity is done. But first, we need to create another line.
Click on the Point Tool on the left hand side again and create a point anywhere on the y-axis again. Select Translate from the Transform menu. On the pop-up menu, you should have your prior numbers on there already. If not, translate this point the same as your last point. Click Translate.

Again, click on the Line Tool on the left hand side and create a new line with the two new points that you have. Select the Arrow Tool on the left hand side, click on any white space, highlight the new line and Measure the Slope of the new line. Click on any white space.

Answer question 11 on your worksheet.
Highlight Point A and Point B. Measure the Coordinate Distance. Click on any white space.
Measure the Coordinate Distance for Point A' and B' as well. Click on any white space.
Answer the rest of the questions on your worksheet. ©

### 3.3.5 Slopes and Stuff on GSP - Optional Investigation

## Worksheet for GSP

| 1. Describe the graph when the slope is <br> greater than 1. | Draw an example. |
| :--- | :--- |
| 2. What is the difference between the <br> slope $=2$ (approximately) and the <br> slope $=6$ (approximately)? | Draw slope $=2$ on the left and draw slope <br> $=6$ on the right. |
| 3. What happens when slope $=0$ ? | Draw an example. |

### 3.3.5 Slopes and Stuff on GSP - Optional Investigation (continued)

6. When you are changing the slope, what stayed the same?
7. What happens when the y-ordinate $\quad$ Draw an example. $=5$ ?
8. What happens when the y-ordinate $\quad$ Draw an example. $=-6$ ?
9. When you are changing the y-ordinate, what stayed the same?
10. In the equation $y=m x+b$, which letter does slope represent? What about the $y$ ordinate?

### 3.3.5 Slopes and Stuff on GSP - Optional Investigation (continued)

| 11. What do you notice about these two lines? |  |
| :--- | :--- |
| 12. What do you notice about the two <br> coordinate distances? | Write down the two coordinate distances <br> here. |
| 13. Because the two coordinate distances <br> are the same, what does that mean <br> about the two lines? | Was your hypothesis correct from question |
|  | 11 ? |

### 3.3.6 Slopes and Stuff Homework

From the graph below, label each point with a name (A, B, etc.), name each slope, state whether the slope is positive or negative, calculate the slope and state any parallel slopes.


Slope: $\qquad$

Slope: $\qquad$

Slope: $\qquad$

Slope: $\qquad$

Slope: $\qquad$

Parallel slopes? $\qquad$

## 3．3．7 Teacher Instructions for Transfrm on the TI－83＋／TI－84

Teacher Instructions for TI－84：

| Press APPS，scroll and find TRANSFRM <br> Press ENTER <br> Press UNINSTALL <br> Press APPS，scroll，find and press TRANSFRM |  |
| :---: | :---: |
| Now you will see．．． Press any key to continue | TEXAS <br> ITFTBTHEFTS <br> TRHHEFORHATIOH <br> GRAPHING <br>  <br> FFESS ADIM HEM <br> T19g9 TEMAS InsTfiUHEITS |
| Blank screen appears again | Cloroe |
| Press $\mathbf{Y}=$ |  |
| Under Y1＝，enter $\mathrm{AX}+\mathrm{B}$ by pressing ALPHA，press MATH，press X，T，，n，press ＋，press ALPHA，press APPS | ```Floti Flote fors H Y 1 \(\mathrm{EF} \mathrm{K}+\mathrm{B}\) HYz= HYる H \(\mathrm{H}_{4}=\) HW5= Hソ面 HY7 =``` |
| Press WINDOWS |  |

### 3.3.7 Teacher Instructions for Transfrm on the TI-83+/TI-84

 (continued)| Scroll up so that SETTINGS is now highlighted and the SETTINGS menu comes on the screen |  |
| :---: | :---: |
| Scroll down until the number beside A is highlighted and enter 1. <br> Enter 1 for B as well. <br> Enter 1 for Step as well. |  |
| Press GRAPH. The equal sign for A is highlighted |  |
| By scrolling to the RIGHT, the value of A will increase and by scrolling to the LEFT, the value of $A$ will decrease |   |
| Scroll DOWN to highlight the equal sign for B. |  |

### 3.3.7 Teacher Instructions for Transfrm on the TI-83+/TI-84

 (continued)| Likewise, scroll RIGHT to increase the value of $B$ and LEFT to decrease the value of $B$. |   |
| :---: | :---: |

### 3.3.8 Teacher Instructions for GSP

Teacher instructions for GSP (slope investigation):


### 3.3.8 Teacher Instructions for GSP (continued)



### 3.3.8 Teacher Instructions for GSP (continued)



## Teacher instructions for GSP (y-intercept investigation):



### 3.3.8 Teacher Instructions for GSP (continued)

| Select Show Grid from the Graph |
| :--- |
| menu. |
| Select the Point Tool. Click anywhere |
| on the y-axis. |
|  |
| Select Translate from the Transform |
| menu. |

### 3.3.8 Teacher Instructions for GSP (continued)



### 3.3.8 Teacher Instructions for GSP (continued)

| Click on Point A and the point that |
| :--- |
| you transformed to create a line. |
| Click on the Select Arrow Tool from |
| the left hand side menu. Click on any |
| white space. Click on the line so that |
| just the line is highlighted. |
| Select Slope from the Measure <br> menu. Click on any white space. |
| Click on the line so that the line is <br> highlighted. Now you can drag the <br> line up and down and the <br> measurement for the y-ordinate will <br> change accordingly. |
| To create parallel lines: <br> Click on the Point Tool on the left <br> hand side menu and create another <br> point on the y-axis. |

### 3.3.8 Teacher Instructions for GSP (continued)



### 3.3.8 Teacher Instructions for GSP (continued)



### 3.3.8 Teacher Instructions for GSP (continued)

| Select Coordinate Distance from the |
| :--- |
| Measure menu. Click on any white |
| space. |
| Click on A' and B' to highlight the two |
| points. |



### 3.4.1 Graphs, Slopes, Intercepts, Equations and Check

One partner will find the y-intercept of each graph and the other partner will find the slope of each graph. You will both then create an equation that represents the graph. Finally, you will check your equation using the graphing calculator (use BLM 3.4.2 as a reference for your graphing calculator).



### 3.4.1 Graphs, Slopes, Intercepts, Equations and Check (Continued)




### 3.4.2 Graphs, Slopes, Intercepts, Equations and Check: Graphing Calculator Keystrokes

1. Prepare your calculator by either running a get-ready program or resetting the graphing calculator.
2. Press the $\xlongequal{\text { WINDOW }}$ button and set the window setting as shown below:
```
WIRTDID
    XMir=-10
    \(\mathrm{M} \cdot \mathrm{x}=16\)
    \(\mathrm{x}=1=1\)
    \(\mathrm{YMir}=-1 \mathrm{~g}\)
    \(\because \mathrm{m} \cdot \mathrm{x}=1 \mathrm{G}\)
```



```
    Xres=1
```

3. To enter an equation for graphing press the
4. Enter your equation in Y1. For example, to graph $y=-3 x-4$ enter:


You will see the following on your screen

|  |  |
| :---: | :---: |

5. To view your graph press the GRAPH button. You will see the graph as shown below:


### 3.4.3 Can Graphing Get Any Easier?

## Investigation 1

$$
y=\frac{1}{3} x+4
$$



1. Start at the y-intercept.
2. Only moving up $(+)$ or down (-), how many units do you need to reach the same level as point B? $\qquad$
3. Only moving right (+), how many units do you have to move your pencil to connect to point $B$ ? $\qquad$
4. Given the equation for the graph state the slope and the y-intercept

Slope $=$ $\qquad$
$y$-intercept $=$ $\qquad$

### 3.4.3 Can Graphing Get Any Easier? (Continued)

## Investigation 2

$$
y=-\frac{4}{5} x+6
$$



1. Start at the y-intercept.
2. Only moving up (+) or down (-), how many units do you need to reach the same level as point B? $\qquad$
3. Only moving right (+), how many units do you have to move your pencil to connect to point $B$ ? $\qquad$
4. Given the equation for the graph state the slope and the y-intercept

Slope $=$ $\qquad$
y-intercept = $\qquad$

### 3.4.3 Can Graphing Get Any Easier? (Continued)

## Investigation 3

$$
y=2 x+5
$$



1. Start at the y-intercept.
2. Only moving up (+) or down (-), how many units do you need to reach the same level as point B? $\qquad$
3. Only moving right (+), how many units do you have to move your pencil to connect to point $B$ ? $\qquad$
4. Given the equation for the graph state the slope and the y-intercept

Slope $=$ $\qquad$
$y$-intercept $=$ $\qquad$

### 3.4.3 Can Graphing Get Any Easier? (Continued)

## Summary

Discuss each question with your partner and both partners write answers.

1. Looking at all three investigations, can you relate the values from steps 2 and 3 with the slope or the y-intercept? Explain the relationship.
2. Given the following equation:

$$
y=\frac{2}{3} x-4
$$

Slope: $\qquad$
$y$-intercept: $\qquad$
Describe a method to graph this equation by hand using the slope and the y-intercept.
3. Using the grid provided below graph the equation $y=\frac{2}{3} x-4$. Write the steps you followed to the right of your graph.


### 3.4.4 Rising and Running From a Point

Graph the following equations on the grids given below and check your graphs using the graphing calculator.

Note: When you write the slope as a fraction, any negative signs should be placed in the numerator only.


### 3.4.4 Rising and Running From a Point (Continued)

Graph the following equations on the grids given below and check your graphs using the graphing calculator.

Note: When you write the slope as a fraction, any negative signs should be placed in the numerator only.


### 3.4.4 Rising and Running From a Point (Continued)

Graph the following equations on the grids given below and check your graphs using the graphing calculator.

Note: When you write the slope as a fraction, any negative signs should be placed in the numerator only.


### 3.4.5: Graphic Organizer



### 3.4.6: Graphic Organizer - Teacher




### 3.5.1: Nspire CAS Handheld Manual

## Getting Started

When you turn on the handheld, press $(\mathbb{\pi})(6)$.
You will be asked whether you want to save the document. Select No. To do this, use the large circular "navpad" to move to the right, then press the風 button.


## 1:Add Calculator

2:Add Graphs \& Geometry
3:Add Lists \& Spreadsheet
4:Add Notes
5:Add Data \& Statistics

Next select 1:Add Calculator. To do this, press the button.
You are now ready to use CAS on the handheld.

## Some Helpful Shortcuts

If you make a mistake at any point that you want to undo, press (2ati).
If you undo something that you want back again, press © © ( )

## How to Solve for a One Variable Equation: Example One

Say that you wish to solve the equation $3 \mathrm{x}+2=14$
To do this, first be certain that you are on a Calculator page. If you need help with this, see the Getting Started section above.

First type in the equation that you want to solve. Use the number pad and the green letter keys; the operations ( $\div, \times,-,+$ ) are located on the right, and the equals sign ( $=$ ) is in the top-left corner of the keypad. When you have typed in the equation, press the key, found in the bottom-right corner.

The top of your screen will look something like this:


Now decide how you would start in solving for $\mathbf{x}$.
Perhaps you've decided that subtracting 2 from both sides of the equation is a good start. Wonderful! To do this, immediately press 3 2 2 . Notice that the handheld automatically inserts Ans. What is this?
Ans stands for the last answer you found. If you now press the eise key, the handheld will subtract 2 from the left side and the right side of $\mathbf{3 x + 2 = 1 4}$. You will see this result:

Continue solving the equation. You probably see that to finally isolate the $\mathbf{x}$ variable, it is necessary to divide the equation by 3 on both sides. Again, just start typing the operation you want to perform. Press [7]. The handheld will insert Ans for you. Press Sis) to calculate the result.

As you can see, the handheld reports that $\mathbf{x}=4$.


| 1.1 | DEG AUTO REAL |
| :--- | ---: |
| $3 \cdot x+2=14$ $3 \cdot x+2=14$ <br> $(3 \cdot x+2=14)-2$ $3 \cdot x=12$ <br> $\frac{3 \cdot x=12}{3}$ $x=4$ |  |

### 3.5.1: Nspire CAS Handheld Manual (Continued)

## How to Solve for a Variable: Example Two

Say that you wish to solve the equation $6 x-5=8$ for the variable $y$.
To do this, first be certain that you are on a Calculator page. If you need help with this, see the Getting Started section above.
First type in the equation that you want to solve. Use the number pad and the green letter keys; the operations ( $\div, \times,-,+$ ) are located on the right, and the equals sign ( $=$ ) is in the top-left corner of the keypad. When you have typed in the equation, press the key, found in the bottom-right corner.

The top of your screen will look something like this:


Now decide how you would start solving for $x$.
Perhaps you've decided that adding 5 to both sides of the equation is a good start. Wonderful! To do this, immediately press $\left\langle\begin{array}{l}7 \\ \hline\end{array}\right\rangle$ [5]. Notice that the handheld automatically inserts Ans. What is this?

Ans stands for the last answer you found. If you now
 side and the right side of $\mathbf{6 x - 5}=\mathbf{8}$. You will see this result:

Continue solving the equation. You probably see that to finally isolate the $\mathbf{x}$ variable, it is necessary to divide the equation by 6 on both sides. Again, just start typing the operation you want to perform. Press (7). The handheld will insert Ans for you. Press Eisiz to calculate the result.

As you can see, the handheld reports that $x=\frac{13}{6}$.

| 1.1 | DEG AUTO REAL |
| :--- | ---: |
| $6 \cdot x-5=8$ | $6 \cdot x-5=8$ |
| Ans+5 |  |
| 1.1 | DEG AUTO REAL |
| $6 \cdot x-5=8$ | $6 \cdot x-5=8$ |
| $(6 \cdot x-5=8)+5$ | $6 \cdot x=13$ |



Is this the result you expected?
To convert this result to its decimal equivalent press ©

Now, try to solve the following equations on your own. Remember to start a new calculator screen for each one.

$$
\begin{aligned}
& 3 x-4=-7 \\
& 7+2 x=4 \\
& -2 x+8=3 x+3
\end{aligned}
$$

### 3.5.1: Nspire CAS Handheld Manual (Continued)

## How to Check a Solution to a One Variable Equation

Say that you have solved the following equation: 6x-5=8
and you believe the solution is $x=\frac{13}{6}$
This would be tedious to check by pencil and paper, but it is quick to check with the handheld.
Here is how to do it. First be certain that you are on a Calculator page. If you need help with this, see the Getting Started section from earlier in this manual.

Here is how to do it:
First type in the equation but do not press 气and The screen looks like:


Next, continue typing by pressing the grey key with the vertical line (1) (in the top row). This symbol means


| 1.1 | DEG AUTO REAL |
| :--- | :--- |
| $6 x-5=8 \mid x=13 / 6$ |  | looks like:

When you press that the solution is correct. If the solution is not correct the handheld will return false.


Now, check your solutions to the three equations you solved on the previous page.

If there are any notes you want to make to help you remember how to solve and check equations use the box below.

### 3.5.2: Temperature Conversions - Investigation

Goal: With a partner you will investigate how to solve one variable equations that have fractional coefficients using CAS and pencil and paper.

Nethead is planning to go to visit Wingman in Detroit. Wingman says that the temperature is $23^{\circ}$ Fahrenheit. Nethead wants to know if he needs to packs warm clothing for his trip. How many degrees Celsius is $23^{\circ}$ Fahrenheit?

We first need a formula that converts Celsius to Fahrenheit. Here's some info to help.

| Temperature in <br> Celsius $(\mathbf{x})$ | Temperature in <br> Fahrenheit $(\mathbf{y})$ |
| :---: | :---: |
| 0 | 32 |
| 20 | 68 |

1. What is the y-intercept? $\qquad$
2. If we write the information as points $(0,32)$ and $(20,68)$, plot the two points and find the slope using a rate triangle.
 Slope $=\frac{\text { rise }}{\text { run }}=$ (Write the slope as a fraction in reduced form.)
3. Now that we know the y-intercept and slope, state the equation relating Celsius ( $\mathbf{x}$ ) to Fahrenheit (y).
4. Using your equation convert the following two temperatures in degrees Celsius to degrees Fahrenheit.
a) $10^{\circ}$
b) $30^{\circ}$

### 3.5.2: Temperature Conversions - Investigation (Continued)

Lets help Nethead now: How many degrees Celsius is it if its $23^{\circ}$ Fahrenheit?
(Hint: Substitute 23 for $\mathbf{y}$ and solve the equation for $\mathbf{x}$ using the Nspire CAS handheld.)
When you enter the equation it will look like:

| 1.1 |
| :--- |
| $23=\frac{9}{5} \cdot x+32$ |

First subtract 32 from both sides
Remember that $\frac{9 x}{5}$ means $\mathbf{x}$ multiplied by 9 and
divided by 5. So, you have to do the opposite of each of the two operations to solve for $\mathbf{x}$.

Your screen will look like:
So $23^{\circ}$ Fahrenheit is $-5^{\circ}$ Celsius.


If we could get rid of the fractions in the equation first you could solve the equation without using CAS. Enter the original equation $23=\frac{9 x}{5}+32$ again and multiply by 5, then subtract and divide to solve. Your solution looks like:

Comparing the two solutions you can see the second one could be done without CAS.

| 1.1 | DEG AUTO REAL |
| :--- | ---: |
| $23=\frac{9}{5} \cdot x+32$ | $23=\frac{9 \cdot x}{5}+32$ |
| $\left(23=\frac{9 \cdot x}{5}+32\right) \cdot 5$ | $115=9 \cdot x+160$ |
| $(115=9 \cdot x+160)-160$ | $-45=9 \cdot x$ |
| $\frac{-45=9 \cdot x}{5}$ | $-9=\frac{9 \cdot x}{5}$ |

5. Convert the following two temperatures in degrees Fahrenheit to degrees Celsius by solving the equation by pencil and paper first and then checking your solution using CAS.
a) $5^{\circ}$
b) $83^{\circ}$
c) $-10^{\circ}$

### 3.5.3: Temperature Conversions - Practice

1. Solve the following equations using pencil and paper.

| a) $\frac{5 x}{3}-4=6$ | b) $\frac{1}{2} x-5=11$ | c) $\frac{4}{5}=\frac{2}{3} x+6$ <br> Hint: Multiply each term by <br> the common denominator |
| :--- | :--- | :--- |

2. Typing Speed: The formula for calculating typing speed is

$$
s=\frac{w}{t}-\frac{10 e}{t} \text { where }\left\{\begin{array}{l}
s \text { is the speed } \\
w \text { is the number of words } \\
t \text { is the time in minutes } \\
e \text { is the number of errors }
\end{array}\right.
$$

a) Nethead types 250 words in 15 minutes with 9 errors. Calculate his typing speed.
b) Wingman types 500 words in 5 minutes and has a typing speed of 72 words per minute. How many errors did he make?


### 3.6.1 Can Three Things Be Really The Same?

$\mathscr{B}$

## Group 1

Models

## Student Cards Below




Algebraic Model

$$
y=10 x+20
$$

Reaiconeran Noses You initially have 20 songs in your iPod and you can download 10 songs per hour.

### 3.6.1 Can Three Things Be Really The Same? (Continued)

$\mathscr{A}$

## Group 2

Models
Student Cards Below
Graphical Model


Algebraic Model

$$
y=20 x
$$

# Real-conext Woosel You are capable of scoring 20 points every game in basketball. 

### 3.6.1 Can Three Things Be Really The Same? (Continued)

$\mathscr{B}$

## Group 3

Models
Student Cards Below
Graphical Model


Algebraic Model

$$
y=-10 x+20
$$

Real-Context Model
A football is initially thrown
from a cliff at a height of 20
m . The ball drops 10 m every
second.

### 3.6.1 Can Three Things Be Really The Same? (Continued)

$\mathscr{H}$
Group 4

Models
Graphical Model

## Student Cards Below



Algebraic Model

$$
y=-10 x+50
$$

Reaiconomex Noses You are given 50 minutes initially cell phone airtime free each month. You use 10 minutes each day.

### 3.6.1 Can Three Things Be Really The Same? (Continued)

$\mathscr{A}$
Group 5

Models
Graphical Model

Student Cards Below


Algebraic Model

$$
y=50 x+10
$$

Real-Context Model

## A person is able to walk 50 metres per minute. The person starts 10 metres from home.

### 3.6.1 Can Three Things Be Really The Same? (Continued)

$\mathscr{A}$

## Group 6

Models
Graphical Model
Student Cards Below


Algebraic Model

$$
y=10 x-50
$$

Real-Context Model
A swimmer is 50 m below sea level. She swims constantly at a rate of 10 metres per minute.

### 3.6.2 Can You Stop The Fire?

## Problem:

You work for the Ministry of Natural Resources as a Fire Fighting supervisor. You arrive in Dryden Ontario where you find two fires burning.

- The first fire has just started along 3 km of shoreline beside a lake and is moving east at a rate of $2 \mathrm{~km} / \mathrm{hr}$.
- The second fire is also rectangular in shape and is being extinguished to the west by fire fighters at a rate of $1 \mathrm{~km} / \mathrm{hr}$.
- Both fires can only change east and west. They will not get wider or narrower.

The picture below shows how the fires looked at the moment you arrived.
Note: Each square $=1 \mathrm{~km}^{2}$


### 3.6.2 Can You Stop The Fire? (Continued)

## Questions:

1. Use the linking cubes to create models that represent the area of both fires at 0,1,2 and 3 hours. Each cube represents $1 \mathrm{~km}^{2}$. Use different colours for the "contained fire" model and the "spreading fire" model.
2. Complete the tables below.

| FIRE 1: The Spreading Fire |  |  |  |
| :---: | :---: | :---: | :---: |
| Time | h (km) <br> (Height) | $\mathbf{w}$ (km) <br> (Width) | A (km <br> (Area) |
| 0 | 3 | 1 |  |
| 1 | 3 |  |  |
| 2 |  |  |  |
| 3 |  |  |  |
| 4 |  |  |  |
| 5 |  |  |  |


| FIRE 2: The Receding Fire |  |  |  |
| :---: | :---: | :---: | :---: |
| Time | $\begin{array}{l}\text { h (km) } \\ \text { (Height) }\end{array}$ | $\begin{array}{l}\mathbf{w} \text { (km) } \\ \text { (Width) }\end{array}$ | $\left.\begin{array}{l}\text { A (km }\end{array}\right)$ |
| (Area) |  |  |  |$)$

3. What variable is the $x$-variable (independent) (Circle one): Time or Area
4. What variable is the $y$-variable (dependent) (Circle one): Time or Area
5. What is the y-intercept (initial value) of both fires:
a. y-intercept of Fire 1: $\qquad$
b. y-intercept of Fire 2: $\qquad$
6. For both sets of data, graph the time vs. the Area of the fires on the grid on the next page and draw lines of best fit for each set of data. Use different colours for each line. Label both axes and each line.

### 3.6.2 Can You Stop The Fire? (Continued)


7. Using the graphs, or the tables, determine the slope (rate of change) of both fires.
a. Slope of Fire 1: $\qquad$
b. Slope of Fire 2:
8. Using the graphs, what is the area of the fires at 6 hours?
a. Area of Fire 1: $\qquad$
b. Area of Fire 2: $\qquad$

### 3.6.2 Can You Stop The Fire? (Continued)

9. Using the values of the slopes and y-intercepts, write an equation of both fires in the form of $y=m x+b$ :
a. Equation of Fire 1: $\qquad$
b. Equation of Fire 2: $\qquad$
10. Using the regression function of the graphing calculator, check to see if your equations are correct. (See 3.6.3 for details.)
11. Using the graphing calculator, check to see if your graphs are correct by graphing both equations. (See 3.6.3 for details.)
12. Using the equations, find the areas of both fires at 6 hours. Compare your answers to the answers from question 9.

Show work for Fire 1

Area of Fire 1 at 6 hours: $\qquad$
Show work for Fire 2

Area of Fire 1 at 6 hours: $\qquad$
13. Looking at both graphs, do the lines ever meet? (Circle one) Yes or No
14. If the lines meet, at what time and area does it occur?
a. Time: $\qquad$
b. Area of Fire: $\qquad$
15. Explain the significance of this point in this context.

### 3.6.3 Can The Graphing Calculator Stop the Fire?

## Determining the Equation of a Line

1. Prepare your calculator by either running a get-ready program or resetting the graphing calculator.
2. Enter the data into the list of the calculator be pressing

## STAT

1 for into L1 and the area of the fire into L2
3. Once all the data has been entered the calculator will perform linear regression to determine the equation of the line of best fit.
4. To determine the equation for the line of best fit press

5. Press to state the two lists to use. Your screen will look like:


## ENTER

6. Now press
$\square$
 to generate the equation. Your screen will show results similar but with different values as below:


Note: a represents the slope.
7. In this case your equation would be: $y=1 x+5$ or $y=x+5$

### 3.6.3 Can The Graphing Calculator Stop the Fire? (Continued)

## Determining the Equation of a Line

8. To view the graph of the data and graph you must first enter the equation of the line in Y 1 by

9. Next enter the equation from above into Y 1:

X,T,Q,n

for $y=x+5$

WINDOW
10. Change the window settings as illustrated below be pressing


GRAPH
11. Now to view the graph press
12. Compare with the graph you made earlier by hand. If they are different check for errors.

### 3.6.4 Modelling Algebraically Problems

Piggy Bank Math
Little Johnny has three dollars to put into his
brand new piggy bank. He will deposit his entire
two-dollar per week allowance into his piggy
bank.
a) Create a table that shows how much little
Johnny will have over the first three weeks.

| Weeks | Balance |
| :--- | :---: |
| 0 <br> (today) | 3 |
| 1 |  |
| 2 |  |
| 3 |  |

b) Create an equation in the form of $y=m x+b$ from the data above.
c) He wants to buy a pet fish that he will name "Ernie" by Christmas, that is, in 9 weeks. Will he have enough money to buy Ernie if he costs $\$ 23$
d) Little Johnny is also considering saving up for a new bike that costs $\$ 127$. If he does not buy the fish, how long will it take until he has saved up enough to buy the bike?
Patterns in Area
Consider the following patterns created with unit
cubes

| Shape \# | Picture | Total Area |
| :--- | :--- | :--- |
| 1 | $\square$ |  |
| 2 | $\square$ |  |
|  | $\square$ |  |
| 3 | $\square$ |  |
| 4 | $\square$ |  |

a) Fill in the picture of $4^{\text {th }}$ shape.
b) Fill in the Total Area Column
c) Create an equation in the form of $y=m x+b$ from the data above.
d) Using your equation, what will the area of $12^{\text {th }}$ figure be? Show your work.
e) How many shapes would you have to build to have 139 cubes? Explain.

### 3.6.4 Modelling Algebraically Problems (Continued)


b) Label the axis in the graph above.
c) Create an equation in the form of $y=m x+b$ from the data above.
d) How much will the mechanic earn after 40 hours
e) How many hours must the mechanic work if she earns $\$ 1240$ ?

Patterns in Area
Consider the following patterns created with unit cubes

a) Build the first, second, third and fourth shapes with the cubes. Fill in the picture of the $4^{\text {th }}$ shape.
b) Fill in the Total Area Column
c) Create an equation in the form of $y=m x+b$ from the data above.
d) What will the area of $7^{\text {th }}$ figure be? Show your work.
e) Can you build the $8^{\text {th }}$ figure? Explain.

### 3.6.5 Consolidation: Four Corners Activity - Teacher

In today's activity, the teacher will read a problem involving linear relations and the students must move to one of the four labelled corners in the classroom.

## Example 1:

Which ordered pair best describes the initial position of the ball?

| 1 | 2 <br> $y=10 x+4$ <br>  <br> A family pays the <br> babysitter $\$ 4.00 / h r$, <br> plus a tip of $\$ 10$ <br> $y=-4 x+10$ |
| :---: | :---: |
|  |  |
| 3 |  |

## Example 2:

Which equation best describes the statement in the middle?

| 1 |  | 2 |
| :---: | :---: | :---: |
| $y=-20 x-3$ |  | $y=20 x-3$ |
|  | You have 20 smarties and are able to 3 every second |  |
| $y=-3 x+20$ |  | $y=-3 x-20$ |
| 3 |  | 4 |

### 3.6.6 Practicing Models

Part A: Complete the following table

| $\#$ | Context | Equation in: <br> $\mathbf{y =} \mathbf{m x}+\mathbf{b}$ | Problem |
| :---: | :--- | :--- | :--- |
| 1 | A caterer charges a flat fee of <br> $\$ 400$ plus $\$ 15 /$ person. |  | Find the cost after 30 people |
| 2 | An internet package charges a <br> flat fee of $\$ 10$ plus $\$ 0.40$ per <br> hour. |  | Find the number of hours of internet usage <br> if the cost is $\$ 200$. |
| 3 | The temperature of hot water <br> placed in the freezer is $80^{\circ} \mathrm{C}$ and <br> it is decreasing at the rate of $8^{\circ} \mathrm{C}$ <br> per hour. |  | Find the temperature after 13 hours. |
| 4 | A tree`s diameter grows by \(13 / 4\) \\ cm per year. The tree`s diameter <br> is currently 12 cm. | Find how many years it will take have <br> diameter $20^{3} / 4 \mathrm{~cm}$. |  |
| 5 | A spring is 14 cm long with no <br> mass on it and it grows by 3 cm <br> per kg put on it. | Find how much weight was added if the <br> spring is 35 cm long. |  |

Part B: For each equation, create a real world context. Identify the independent variable ( $\mathbf{x}$ ) and dependent variable ( $\mathbf{y}$ ) for each.

1. $y=15 x$
2. $y=0.05 x+25$ $\qquad$
$\qquad$
3. $y=20 x-100$ $\qquad$
$\qquad$


### 3.7.1 Y the X Are You Intercepting Me?

On the grid paper on the next page plot and label all the points listed below.
(Note: Each point is labelled so you can refer to them later.)

| $\mathrm{A}(3,3)$ | $\mathrm{B}(2,3)$ | $\mathrm{C}(1,3)$ | $\mathrm{D}(0,3)$ | $\mathrm{E}(-1,3)$ | $\mathrm{F}(-2,3)$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{G}(-3,3)$ | $\mathrm{H}(3,2)$ | $\mathrm{I}(3,1)$ | $\mathrm{J}(3,0)$ | $\mathrm{K}(3,-1)$ | $\mathrm{L}(3,-2)$ |
| $\mathrm{M}(3,-3)$ | $\mathrm{N}(-3,2)$ | $\mathrm{O}(-3,1)$ | $\mathrm{P}(-3,0)$ | $\mathrm{Q}(-3,-1)$ | $\mathrm{R}(-3,-2)$ |
| $\mathrm{S}(-3,-3)$ | $\mathrm{T}(2,-3)$ | $\mathrm{U}(1,-3)$ | $\mathrm{V}(0,-3)$ | $\mathrm{W}(-1,-3)$ | $\mathrm{X}(-2,-3)$ |

Now, read the following carefully. There are three columns given: starting point, ending point and slope.

- If you have the starting point and slope, you have to state the ending point.
- If you have the ending point and slope, you have to state the starting point.
- If you have the starting point and ending point, you have to state the slope.

| Starting Point | Ending Point | Slope |
| :---: | :---: | :---: |
| G |  | $-1 / 6$ |
| F |  | $-2 / 5$ |
| E | J |  |
| O | X | $-4 / 3$ |
| Q | T | -6 |
| B | M |  |
| D | M | $-5 / 2$ |
| N | U | $-5 / 2$ |
| R | A |  |
| C | M |  |
| P | S |  |
| S | M |  |
| G |  |  |
| A |  |  |

Making the picture:
Connect each starting point to each ending point.
What type of shape is created?

State the y-intercepts:

State the x-intercepts:

### 3.7.1 Y the X Are You Intercepting Me ? (Continued)



### 3.7.2 Teacher Notes for Guided Investigation

Guide students to see that when given two points, connecting the points to create a line is easy and possible.

From yesterday's lesson, students know how to write an equation of a line when given a graphical representation. Thus, with a graph that students create with two given points, students will be able to write an equation of a line easily.

Introduce the Standard Form Ax $+\mathrm{By}+\mathrm{C}=0$. It is because of the Standard Form that recognizing the $x$ - and $y$-intercepts are important.

Demonstrate how to solve for y -intercept. Again, refer back to what students found out about y intercepts from today's lesson - i.e. all $y$-intercepts have an $x$-value of 0 . Thus, by substituting $x$ $=0$ into the Standard Form of an equation, students can solve for $y$, and as a result, students can obtain the y-intercept.

Example: $2 x+4 y+8=0$
To find the $y$-intercept, substitute $\mathrm{x}=0$ into the equation. So,
$2(0)+4 y+8=0$
$0+4 y+8=0$
$4 y+8=0$
$4 y=-8$
$y=-8 / 4$
$y=-2$

Likewise, demonstrate how to solve for the x-intercept. Again, refer back to what students found out about $x$-intercepts from today's lesson - i.e. all x-intercepts have an $y$-value of 0 . Thus, by substituting $y=0$ into the Standard Form of an equation, students can solve for $x$, and as a result, students can obtain the x-intercept.

Example: $2 x+4 y+8=0$
To find the $x$-intercept, substitute $y=0$ into the equation. So,

| $2 \mathrm{x}+4$ (0) | $+8=0$ |
| :---: | :---: |
| $2 \mathrm{x}+0$ | $+8=0$ |
| 2 x | $+8=0$ |
| 2x | = -8 |
| x | = -8/2 |
| x | $=-4$ |

Conclude by reminding students that finding the x - and y -intercepts is easy. As a result, students can create a line with the two points, and can write an equation of a line based on the line that they have.

### 3.7.3 Y the X Are You Intercepting Me - Practice

Answer the following questions based on the lines graphed below.

1. Which lines have positive slopes?
2. Which lines have negative slopes?
3. Fill in the table by listing the coordinates for the $x$ intercepts and y-intercepts.


| Line | $x$-intercepts | $y$-intercepts |
| :---: | :---: | :---: |
| 1 |  |  |
| 2 |  | $(0,6)$ |
| 3 |  |  |
| 4 | $(-4,0)$ |  |

4. Write the equation for line \#1.
5. Write the equation for line \#2.
6. Write the equation for line \#3.
7. Write the equation for line \#4.

### 3.7.3 Y the X Are You Intercepting Me - Practice (Continued)

8. Calculate the $x$ and $y$-intercepts and graph each line on the graph paper on the next page.
a) $3 x-2 y-6=0$
b) $5 x+2 y-10=0$
c) $3 x-y-9=0$
d) $2 x-5 y-14=0$

### 3.7.3 Y the X Are You Intercepting Me - Practice (Continued)



| Unit 3 Day 8: Slopes Away |  | Grade 10 <br> Applied |
| :---: | :---: | :---: |
| Minds On: 20 Min. | Math Learning Goals <br> Students will: <br> - Determine the equation of a line, given the slope and $y$-intercept <br> - Given two points, write the equation of a line. <br> - Determine the slope of the line using rate triangles and the formula. | Materials <br> - BLM 3.8.1 - 3.8.4 |
| Action: $\quad 35 \mathrm{Min}$. <br> Consolidate $/$ <br> Debrief: $\quad 20 \mathrm{Min}$ |  |  |
| Total $=75 \mathrm{Min}$ |  |  |
| Assessment Opportunities |  |  |
| Minds On... | Individual $\rightarrow$ Activating Prior Knowledge <br> Students review concepts learned so far in the unit using BLM 3.8.1. <br> Curriculum Expectations/Observation/Quiz: Assess students' knowledge of linear systems. | Two colour counters may be used to help students who have difficulty subtracting integers. <br> Teacher may wish to introduce $m=\frac{y_{2}-y_{1}}{x_{2}-x_{1}} \text { after }$ <br> students have defined their own method of calculating slope. |
| Action! | Pairs $\rightarrow$ Think/Pair/Share <br> Students work on each question on BLM 3.8.2 individually and then compare their solutions with a partner. Students write their own method for determining slope given two points. <br> Strategy for Undefined Slope: Slope can be thought of as a measure of the difficulty of walking up an incline. A horizontal incline has zero difficulty. As the incline becomes steeper the difficulty increases. When the incline is vertical it is impossible to walk up it so the slope cannot be defined. <br> Pairs $\rightarrow$ A Coaches B <br> Students complete BLM 3.8.3. Partners alternate coaching to provide feedback. |  |
| Consolidate Debrief | Individual and Whole Class $\rightarrow$ Investigation <br> Students will continue with their new knowledge of calculating slope algebraically to write the equation of the line using BLM 3.8.4 | Students can use a graphing calculator or CAS to verify their answers. |
| Practice | Home Activity or Further Classroom Consolidation Additional practice can be given as needed. |  |
|  |  |  |

### 3.8.1 Writing Equations of Lines

## Working with Another Form

## Some Review

1. What is the slope and $y$-intercept for each line?
a) $y=-3 x+1$
b) $y=\frac{3}{4} x-3$
$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$
$\mathrm{m}=$ $\qquad$ $\mathrm{b}=$ $\qquad$
2. Using this information, graph each of the equations on the grid below. Use a different colour for each line and label each line.

3. Let's look at another two equations.
a) $3 x+y-1=0$
b) $3 x-4 y-12=0$

What are two things you notice are different about these equations when you compare them to the equations in \#1?

## REMINDER:

You can only read the slope and y-intercept from the equation of a line if it is in $\boldsymbol{y}=\boldsymbol{m} \boldsymbol{x} \boldsymbol{+} \boldsymbol{b}$ form.

### 3.8.1 Writing Equations of Lines (Continued)

4. Calculate the $x$-intercept and the $y$-intercept. Then graph the equations on the grid below. Use a different colour for each line and label each line.
a) $3 x+y-1=0$
b) $3 x-4 y-12=0$

## Practice:

5. For each equation:
$>$ Calculate the x-intercept and the y-intercept.
$>$ Graph on the grid provided. Use a different colour for each line and label each line.
a) $2 x+y-4=0$
b) $4 x+2 y+6=0$


### 3.8.2: Jack and Jill Go up a Hill

## For each of the following questions

a) Plot the points on the given grid.
b) Draw a line connecting the points
c) Calculate the rise by counting squares. Calculate the rise again by using the coordinates of the points. Show your work to confirm your answers. (The first one is done for you).
d) Calculate the run by counting squares. Calculate the run again by using the coordinates of the points. Show your work to confirm your answers.
e) Calculate the slope. (rate of change)


| 1. $\mathbf{A}(0,3) \mathbf{B}(2,0)$ | 2. $C(-2,0) \quad D(0,5)$ | 3. $\mathrm{E}(3,0) \mathrm{F}(0,-7)$ | 4. $\mathbf{G}(0,0) \mathbf{H}(7,0)$ |
| :---: | :---: | :---: | :---: |
| Rise: $3-0=3$ | Rise: | Rise: | Rise: |
| Run: $0-2=-2$ | Run: | Run: | Run: |
| $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ |

### 3.8.2: Jack and Jill go up a Hill (Continued)



| 5. $\mathbf{A}(2,3) \mathbf{B}(5,0)$ | 6. $\mathbf{C}(-2,1) \mathbf{D}(3,5)$ | 7. $\mathbf{E}(2,1) \mathbf{F}(3,6)$ | 8. $\mathbf{G ( - 3 , - 3 ) \mathbf { H } ( - 3 , 7 )}$ |
| :--- | :--- | :--- | :--- |
| Rise: | Rise: | Rise: | Rise: |
| Run: | Run: | Run: | Run: |
| Slope $=\frac{\text { Rise }}{\text { Run }}$ | Slope $=\frac{\text { Rise }}{\text { Run }}$ | Slope $=\frac{\text { Rise }}{\text { Run }}$ | Slope $=\frac{\text { Rise }}{\text { Run }}$ |

Describe in your own words how you would calculate the slope of a line given two points without using a graph.

### 3.8.3: Slopes "A" way

| A Coaches B | B Coaches A |
| :---: | :---: |
| 9. A $(25,30) \mathrm{B}(35,20)$ | 10. E (-13, -23) F (31, 17) |
| $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ |
| 11. G (32, 21) H (-3, -16) | 12. $\mathrm{A}(7,40) \mathrm{B}(11,81)$ |
| $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ |
| 13. E (3, 33) F $(2,27)$ | 14. G (-200, -100) H (30, -6) |
| $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ |
| 15. E (-12, -15) F (-20, -4) | 16. $\mathrm{E}(5,-6) \mathrm{F}(15,8)$ |
| $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ | $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ |

### 3.8.4: Writing Equations of Lines

For each of the following questions:

1. Plot the points on the given grid.
2. Draw a line connecting the points and extend the line in both directions to the edge of the graph.
3. Calculate the slope (rate of change) using a formula. Compare your answer with your graph.
4. Using the graph state the y-intercept.
5. Write the equation of the line in slope $y$-intercept form.

6 . Verify your equation using a graphing calculator.


### 3.8.4: Writing Equations of Lines (Continued)

For each of the following questions:

1. Plot the points on the given grid.
2. Draw a line connecting the points and extend the line in both directions to the edge of the graph.
3. Calculate the slope (rate of change) using the formula. Compare your answer with your graph.
4. Using the graph state the y-intercept.
5. Write the equation of the line in slope y-intercept form.
6. Verify your equation using a graphing calculator.


7. $\mathrm{A}(-2,-2) \mathrm{B}(2,10)$

Slope $=\frac{\text { Rise }}{\text { Run }}$
$y$-intercept $=$

Equation:
4. $\mathrm{A}(4,-6) \mathrm{B}(12,0)$

Slope $=\frac{\text { Rise }}{\text { Run }}$
$y$-intercept $=$

Equation:

### 3.8.4 Writing Equations of Lines (Continued)

For each of the following questions:

1. Plot the points on the given grid.
2. Draw a line connecting the points and extend the line in both directions to the edge of the graph.
3. Calculate the slope (rate of change) using the formula. Compare your answer with your graph.
4. Using the graph state the y-intercept.
5. Write the equation of the line in slope $y$-intercept form.
6. Verify your equation using a graphing calculator.

| - |  |  |  |  |  | fr |  |  |  |  | 5. A $(-6,4) \mathrm{B}(5,4)$ $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ <br> y -intercept $=$ <br> Equation: |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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|  |  |  |  |  |  |  |  |  | - | - |  |  |
|  |  |  |  |  |  |  |  |  |  |  | 6. $A(-6,1) B(12,4)$ $\text { Slope }=\frac{\text { Rise }}{\text { Run }}$ <br> $y$-intercept $=$ <br> Equation: |  |
|  |  |  |  |  |  | ${ }^{+}$ |  |  |  |  |  |  |
|  |  |  |  |  |  | f |  |  |  |  |  |  |
|  |  |  |  |  |  | ${ }^{1}$ |  |  | - | - |  |  |
|  |  |  |  |  |  | ${ }^{7}$ |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  | 2-1-10 | ¢ | ${ }_{6}^{-6}$ | 4 | -2-1-1 |  | $2^{3}{ }^{4}$ |  |  |  |  |  |
|  |  |  |  |  | - |  |  |  |  | $\square$ |  |  |
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### 3.9.1: Solving Equations - Teacher

| Equation 1 | Equation 2 | Equation 3 |
| :---: | :---: | :---: |
| $10=3 x-2$ | $-33=5 x+7$ | $0=2 x+6$ |
| $10+2=3 x-2+2$ | $-33-7=5 x+7-7$ | $0-6=2 x+6-6$ |
| $12=3 x$ | $-40=5 x$ | $-6=2 x$ |
| $\frac{12}{3}=\frac{3 x}{3}$ | $\frac{-40}{5}=\frac{5 x}{5}$ | $\frac{-6}{2}=\frac{2 x}{2}$ |
| $4=x$ | $-7=x$ | $-3=x$ |
| Equation 4 | Equation 5 | Equation 6 |
| $15=14+b$ | $36=-3+b$ | $43=-10 x-11$ |
| $15-14=14-14+b$ | $36+3=-3+3+b$ | $43+11=-10 x-11+11$ |
| $1=b$ | $39=b$ | $54=-10 x$ |
| $\frac{54}{-10}=\frac{-10 x}{-10}$ | $\frac{-27}{5}=x$ | $-5.4=x$ |

### 3.9.2 Yes, We got no Graph Paper!

Given points, the slope and/or the $y$-intercept, write the equation in $y=m x+b$ form for each of the following:

| A coaches B | B coaches A |
| :---: | :---: |
| Given: <br> slope $=5, y$-intercept $=5$ | Given: $M=-2, b=3$ |
| Equation: | Equation: |
| Given: <br> Slope parallel to $y=2 x-7$ with the same $y$ intercept as $\mathrm{y}=4 \mathrm{x}-10$ | Given: <br> Slope parallel to $x=5$ going through point A $(2,5)$ |
| Equation: | Equation: |
| Given: <br> Slope is $0, y$-intercept $=5$ | Given: $\text { slope }=4, \text { Point A }(0,3)$ |
| Work Shown: | Work Shown: |
| Equation: | Equation: |
| Given: <br> Point A (4, 3), Point B (-1, 3) | Given: <br> Point A $(0,-1)$, Point B $(4,8)$ |
| Work Shown: | Work Shown: |
| Equation: | Equation: |
| Given: $\text { Slope }=\frac{3}{5}, \text { Point }(5,7)$ | Given: $M=\frac{-5}{3}, \text { Point } A(5,0)$ |
| Work Shown: | Work Shown: |
| Equation: | Equation: |

### 3.9.2 Yes, We got no Graph paper! (Continued)

Given two points, the slope and/or the $y$-intercept, write the equation in $y=m x+b$ form for each of the following:

| A coaches B | B coaches A |
| :---: | :---: |
| Given: <br> Point A (10, 19), Point B (18, 31) | Given: <br> Point A $(4,6)$, Point B $(7,15)$ |
| Work Shown: | Work Shown: |
| Equation: | Equation: |
| Given: <br> Point A $(5,0)$, Point B $(0,200)$ | Given: <br> Point A $(0,5)$, Point B $(200,0)$ |
| Work Shown: | Work Shown: |
| Equation: | Equation: |
| Given: <br> Point A (1.5, 6.5), Point B (-1.5, -2.5) | Given: <br> Point A (1, 8.50), Point B (4, 28.50) |
| Work Shown: | Work Shown: |
| Equation: | Equation: |

### 3.9.3: I'm on your side.

You will be assigned one of four shapes. Your job is to find the equation relating the number of shapes and the number of sides and then answer some other questions.

## SQUARE INVESTIGATION

Start by placing squares side by side as shown. Note: This arrangement of 4 squares has 13 sides.


1. Complete the following table relating the number of squares and total number of sides.

| Number of <br> squares (n) | Number of <br> sides (s) |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 | 13 |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |

Equation: s = $\qquad$ $\mathrm{n}+$ $\qquad$
(Remember: You need the slope and $y$-intercept. Use your knowledge to calculate these values.)
2. Use your equation to calculate the number of sides that 50 squares placed side by side would have.
3. Use your equation to calculate how many squares you would have if you counted all the sides and got a number of sides equal to 256 ?

### 3.9.3: I'm on your side. (Continued)

## RECTANGLE INVESTIGATION

Start by placing rectangles side by side as shown. Note: This arrangement of 4 rectangles has 13 sides.


1. Complete the following table relating the number of rectangles and total number of sides.:

| Number of <br> rectangles ( $\mathbf{n}$ ) | Number of <br> sides (s) |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 | 13 |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |

Equation: s = $\qquad$ n + $\qquad$
(Remember: You need the slope and $y$-intercept. Use your knowledge to calculate these values.)
2. Use your equation to calculate the number of sides that 75 rectangles placed side by side would have.
3. Use your equation to calculate how many rectangles you would have if you counted all the sides and got a number of sides equal to 724 ?

### 3.9.3: I'm on your side. (Continued)

## HEXAGON INVESTIGATION

Start by placing hexagons side by side as shown. Note: This arrangement of 2 hexagons has 11 sides.


1. Complete the following table relating the number of hexagons and total number of sides.

| Number of <br> hexagons ( $\mathbf{n}$ ) | Number of <br> sides (s) |
| :---: | :---: |
| 1 |  |
| 2 | 11 |
| 3 |  |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |

Equation: s = $\qquad$ n + $\qquad$
(Remember: You need the slope and $y$-intercept. Use your knowledge to calculate these values.)
2. Use your equation to calculate the number of sides that 76 hexagons placed side by side would have.
3. Use your equation to calculate how many hexagons you would have if you counted all the sides and got a number of sides equal to 1206 ?

### 3.9.3: I'm on your side. (Continued)

## TRIANGLE INVESTIGATION

Start by placing triangles side by side as shown. Note: This arrangement of 3 triangles has 11 sides.


1. Complete the following table relating the number of triangles and total number of sides.

| Number of <br> triangles ( $\mathbf{n}$ ) | Number of <br> sides (s) |
| :---: | :---: |
| 1 |  |
| 2 |  |
| 3 | 7 |
| 4 |  |
| 5 |  |
| 6 |  |
| 7 |  |

Equation: s = $\qquad$ $\mathrm{n}+$ $\qquad$
(Remember: You need the slope and $y$-intercept. Use your knowledge to calculate these values.)
2. Use your equation to calculate the number of sides that 76 triangles placed side by side would have.
3. Use your equation to calculate how many triangles you would have if you counted all the sides and got a number of sides equal to 483 ?

### 3.9.4: I'm on your side.

Your best friend has called you for help on writing equations of lines. They have been given two points. Explain to them two different ways to write the equation of the line. You may use words, numbers or graphs in your explanation.

| Unit 3 Day 10: So, You Think You Know Everything About Lines? |  | Grade 10 <br> Applied |
| :---: | :---: | :---: |
| Minds On: 15 Min. | Math Learning Goals <br> Students will: <br> - Review x - and y -intercepts. <br> - Investigate the special cases $x=a$ and $y=b$. <br> - Express the equation of a line in the form $\mathrm{y}=\mathrm{mx}+\mathrm{b}$, given the form $\mathrm{ax}+$ by $+c=0$. | Materials <br> - BLM 3.10.1- <br> 3.10.6 |
| Action: 40 Min. |  |  |
| Consolidate/ Debrief: 20 Min |  |  |
| Total $=75$ Min. |  |  |
|  | Assessment Opportunities |  |
| Minds On... | Pairs $\rightarrow$ Review Intercepts Worksheet <br> Distribute BLM 3.10.1. Students activate prior knowledge by completing the worksheet. <br> Whole Class $\rightarrow$ Discussion <br> Share student solutions and discuss student's findings. |  |
| Action! | Pairs $\rightarrow$ Investigation <br> Distribute BLM 3.10.2 to the Horizontal group. Distribute BLM 3.10.3 to the Vertical group. Have students complete the worksheets in pairs. <br> Pairs $\rightarrow$ A Coaches B <br> Pairs coach their partner on the investigation they completed. Partner being coaches completes the appropriate BLM. Pairs switch roles and repeat for the other investigation. <br> Whole Class $\rightarrow$ Teacher Led Lesson <br> Using BLM 3.10.5 teach students how to convert from standard form of an equation to slope y-intercept form using prior knowledge on solving one variable equations using algebra. | Refer to BLM 3.10.4 for directions on how to pair students for the two paired activities. |
| Consolidate Debrief | Whole Class $\rightarrow$ Discussion <br> Consolidate student understanding on: <br> - horizontal and vertical lines <br> - converting from Standard Form to slope y-intercept form |  |
| Concept Practice | Home Activity or Further Classroom Consolidation <br> Students complete BLM 3.10.6 for further practice. | Use an exit ticket that has students make up their own Standard Form equation and convert it to slope $y$ intercept form. |

### 3.10.1: So, You Think You Know Everything About Lines? Review of Concepts

You've learned a lot up to this point in the unit, and to ensure that you still remember it, let's do a little review. With your partner complete the following questions. Feel free to consult your notebook if you cannot remember.

| 1. What is a y-intercept? What is an x- <br> intercept? | Give an example of each (in coordinate form). |
| :--- | :--- |
| 2. Give an example of an equation in |  |
| Standard Form. | How does the Standard Form make graphing <br> easier for you? |
| 3. If you graph the line using the Standard |  |
| Form, how many intercepts do you have? | Can you graph a line any other way so that it <br> will only have 1 intercept? (If so, sketch an <br> example below.) |
| 4. Is it possible to graph a line so that it will |  |
| have no intercepts? Explain. |  |$\quad$| Is it possible to have more than 2 intercepts? |
| :--- |
| Explain. |

### 3.10.2: So, You Think You Know Everything About Lines? Horizontal Lines Investigation

With your partner complete the investigation below. You will be asked to coach someone later.

1. For the graph below, write the coordinates of each point on the graph in the table below.

$\qquad$
C ( $\qquad$ , $\qquad$ )

D $\qquad$ , $\qquad$ )

E $\qquad$ , $\qquad$ )

F ( $\qquad$ , $\qquad$
G ( $\qquad$ , $\qquad$ )
2. What do all the points have in common?
3. There is only one point that has a coordinate of zero. What is another name for this point?

### 3.10.2: So, You Think You Know Everything About Lines? Horizontal Lines Investigation (Continued)

4. What is the equation of the line joining all the points? (Hint: The slope of the line is zero so the equation only depends on the value of the $y$ intercept.)
5. What if all the points from the graph in question 1 shift up 2 units. What will your equation be now?
6. What if all the points from the graph in question 1 shift down 4 units. What will your equation be now?
7. Write the equation of the horizontal line that passes through:
a) $(3,4)$
b) $(-2,-4)$
c) $(2.0)$
8. Write a general equation for all horizontal lines? (Hint: Use b for the y-intercept)

### 3.10.3: So, You Think You Know Everything About Lines? Vertical Lines Investigation

With your partner complete the investigation below. You will be asked to coach someone later.

1. For the graph below, write the coordinates of each point on the graph in the table below.

2. What do all the points have in common?
3. There is only one point that has a coordinate of zero. Is there another name for this point?

### 3.10.3: So, You Think You Know Everything About Lines? Vertical Lines Investigation (Continued)

4. What is the equation of the line joining all the points? (Hint: The slope of the line is undefined so the equation only depends on the value of the $x$ intercept.)
5. What if all the points from the graph in question 1 shift right 2 units. What will your equation be now?
6. What if all the points from the graph in question 1 shift left 4 units. What will your equation be now?
7. Write the equation of the vertical line that passes through:
a) $(3,4)$
b) $(-2,-4)$
c) (0.-1)
8. Write a general equation for all vertical lines? (Hint: Use a for the x-intercept)

### 3.10.4: Teacher Notes

## Pairing Strategy for Horizontal and Vertical Lines Activities

Split the class into 2 heterogeneous groups with an equal number of students in each group. Name one group Horizontal, name the other Vertical.

Have each student in the Horizontal group spread their arms wide. Students measure their arm length against one another and arrange themselves in descending order (from widest arm span to shortest arm span). Then group students into pairs by starting with the student with the widest arm length. This student will be partner with the person next to him/her. The third person will be partner with the fourth person, and so on. If the group has uneven numbers, then have a group of three at the end.

Have each student in the Vertical group raise their arms straight over their heads. Students measure their vertical arm length against one another and arrange themselves in descending order (from the tallest overhead arm length to the shortest overhead arm length). Then group students into pairs by starting with the student with the tallest arm length. This student will be partner with the person next to him/her. The third person will be partner with the fourth person, and so on. If the group has uneven numbers, then have a group of three at the end.

## Pairing Strategy for A Coaches B

The student with the widest arm span will pair with the student with the tallest arm length for the coaching activity. The partner of the student with the widest arm span will pair with the partner of the student with the tallest arm length. The third student in arm span will pair with the third student in arm length and so on.

Students with the completed horizontal worksheets will be Partner A. Students with the completed vertical worksheets will be Partner B.

Partner A will coach Partner B about horizontal lines. Partner B will coach Partner A about vertical lines.

### 3.10.6: Teacher Notes - Converting from Standard Form to Slope Y-intercept Form

There are times when an equation in Standard Form needs to be converted to an equivalent equation in Slope Y-intercept Form.

| The advantages of Standard Form $(A x+B y+C=0)$ | The disadvantages of Standard Form (Ax $+\mathrm{By}+\mathrm{C}=0$ ) |
| :---: | :---: |
| - $\quad x$ and $y$ intercepts can quickly be determined | - rate of change (slope) is not immediately known |
| - graph can be quickly made | - fixed amount (y-intercept) is not immediately known |

Using what we learned about solving equations in this unit we can convert an equation from Standard Form to Slope Y-Intercept Form. Here's how:

1. Write the equation in standard form
2. Isolate the term containing $y$ by adding or subtracting to both sides the term containing the $x$ term
3. Complete isolation of the term containing y by adding or subtracting to both sides the term containing the number term
4. Divide both sides of the equation by coefficient of the term containing $y$. If the division does not result in an integer write terms with fractions in lowest terms.

Example 1:
$2 x+3 y+6=0$
$2 x+3 y+6-2 x=0-2 x$
$3 y+6-6=-2 x-6$
$3 y=-2 x-6$
$y=-2 / 3 x-6 / 3$ (because the whole right hand side is being divided by 3 )
$y=-2 / 3 x-2$ (simplify)

## Example 2:

$6 x+3 y-12=0$
$6 x+3 y-12-6 x=0-6 x$
$3 y-12+12=-6 x+12$
$3 y=-6 x+12$
$y=-6 / 3 x+12 / 3$
$y=-2 x+4$ (point out to students that sometimes the numbers work out nicely, but if not, then leave the numbers in fractions form)

```
Example 3:
\(-4 x-5 y-7=0\)
\(-4 x-5 y-7+4 x=0+4 x\)
\(-5 y-7+7=4 x+7\)
    \(-5 y=4 x+7\)
        \(y=4 / 5 x+7 / 5\) (because the fractions cannot be reduced, leave them as they are)
```


### 3.10.6 Converting from Standard to Slope Y-Intercept Form Practice

1. Convert the equations below into slope y-intercept form.
a) $3 x+y-1=0$
b) $3 x-4 y-12=0$
2. Now, state the slope and y-intercept for each equation.
a)
b)
$\mathrm{m}=$ $\qquad$ $b=$ $\qquad$ $\mathrm{m}=$ $\qquad$ $b=$ $\qquad$
3. For each equation:
> Convert to slope y-intercept form
$>$ State the slope and $y$-intercept.
$>$ Graph on the grid provided. Use a different colour for each line. Label each.
a) $2 x+y-4=0$
b) $4 x+2 y+6=0$
c) $x-y-5=0$
d) $3 x+2 y-8=0$
$\mathrm{m}=$ $\qquad$ $b=$ $\qquad$
$\mathrm{m}=$ $\qquad$ $b=$
$m=$ $\qquad$ $\mathrm{b}=$ $\qquad$
$\mathrm{m}=$ $\qquad$ b $=$ $\qquad$


| Unit 3 Day 11: London Bridge Is Falling Down... |  | Grade 10 Applied |
| :---: | :---: | :---: |
| Minds On: 5 Min. | Math Learning Goals <br> Students will: <br> - Collect data on linear relations in context of real-life problems <br> - Determine the equation of the linear relation <br> - Relate the slope and intercepts in the context of real-life applications | Materials <br> - Graphing |
| Action: 60 Min . |  | Calculators (optional) |
| Consolidate/ Debrief: 5 Min |  | - 200 Linking Cubes or pennies |
| Total $=75 \mathrm{Min}$. |  | - Scissors |
| Assessment Opportunities |  |  |
| Minds On... | Groups $\rightarrow$ Matching Models <br> Students are given cards from BLM 3.11.1. Each student will receive either an equation in $\mathrm{y}=\mathrm{mx}+\mathrm{b}$, a slope/ y -intercept, or an equation in standard form. Once all the cards are given out, students are to form groups with other students whose cards represent the same line. (3 in a group). | Teacher should have BLM 3.11.1 cut out before class. Make sure the cards are mixed up before handing the cards out. |
|  |  | Some website you can observe on |
|  | The teacher may want to introduce this activity though discussion on bridge design and what determines what a good bridge design (you may use BLM 3.11.2 or various websites). <br> Students will work in groups of 3 based on the grouping from BLM 3.11.1. Each group member will have a task based on their Minds On card. Students will collect data relating the layers in the bridge to the number of cubes it takes for the bridge to collapse. Students record their data on (BLM 3.11.3). If students do not get linear data, BLM 3.11.4 can be an intervention. <br> Students will then use their data to create a scatter plot, determine equations of the line of best fit fro both bridge models. They will then extrapolate and interpolate various values from their algebraic model and identify the significance of the slope in the context. Students will then answer various questions involving the standard form of a line, and intercepts. <br> Students can also hand this activity in as part of their summative assessment for unit 3. Calculators can also be used to verify their equations. <br> Mathematical Process Focus: Connecting (Students will connect, slope, intercepts and equations to real-life contexts) | bridges: <br> http://www.pbs.org/w gbh/nova/bridge/ or http://www.scienceb uddies.org/science-fairprojects/project_idea s/CE_p011.shtml?fr om=Home <br> It might be better to cut all the paper you need a head of time (BLM 3.11.3). You will need 6 halves for each group <br> If linking cubes are not present you might want to use pennies. <br> It would be better to use 12 oz large plastic cups |
| Consolidate Debrief | Whole Class $\rightarrow$ Sharing <br> Take up the review questions from lesson 3.10. Students share a variety of solutions to homework problems. Identify and address any misconceptions. | A possible extension is for students to create a different bridge model an perform the cube collapse test. |
| Concept Practice Application | Home Activity or Further Classroom Consolidation <br> Students work on the unit review to prepare for the unit summative assessment task or a pencil and paper test. | A sample unit summative task is found in unit 8 in the members area of the OAME web site. |

### 3.11.1: Hand In Hand Together -Teacher Note

- Each student will receive a card listed below, copied onto an index card or cut into sections in advance.
- Organize the classroom so that all slopes are located in one area, all $y=m x+b$ cards are located in another area etc. with a row of single desks separating each group (see diagram below).
- Students are to remain in their area and can only speak with the group directly beside them. Thus, Slope \& y-intercept students can talk to both groups but Y-intercept Slope Form students can't speak with the Standard Form students. They will need to cooperate with each other to find their proper matches.
- Once they have found their matches they are to hold hand in hand across the desks to form a bridge.
- Note: You might want to consider giving the stronger students the middle card.


## Classroom Set Up:

| Y-intercept Slope Form | Desk | Slope \& Y-intecept Students | Desk | Standard Form |
| :---: | :---: | :---: | :---: | :---: |
|  | Desk |  | Desk |  |
| Students |  |  |  | Students |

Cards:

| Y-intercept Slope | Slope \& Y-intercept | Standard |
| :---: | :---: | :---: |
| $y=\frac{-3}{2} x+2$ | $m=\frac{-3}{2},(0,2)$ | $3 x+2 y-4=0$ |
| $y=\frac{5 x}{3}+2$ | $m=\frac{5}{3},(0,2)$ | $5 x-3 y+6=0$ |
| $y=\frac{-3 x}{2}+4$ | $m=\frac{-3}{2},(0,4)$ | $3 \mathrm{x}+2 \mathrm{y}-8=0$ |
| $y=\frac{5 x}{3}-3$ | $m=\frac{5}{3},(0,-3)$ | $5 x-3 y-9=0$ |
| $y=\frac{-x}{4}+4$ | $m=\frac{-1}{4},(0,4)$ | $x+4 y-16=0$ |
| $y=\frac{-x}{4}-3$ | $m=\frac{-1}{4},(0,-3)$ | $x+4 y+12=0$ |

### 3.11.2 London Bridge Is Falling Down...Introduction

## Introduction to Bridge Building

There are many different types of bridge designs which serve different purposes. The factors that determine the bridge design includes the type of traffic (i.e. more trucks or cars), what is under the bridge, the aesthetics and the cost.
Cable-Stayed Bridge

Source: Images are taken from: NOVA Online http://www.pbs.org/wgbh/nova/bridge/build.html

Before a bridge is constructed, engineers design models to ensure that the bridge can withstand the stress of the load from cars and people.

In today's activity, you will be working in groups of three. Your group will construct two bridge designs out of paper: the Plank Bridge and the Arch Bridge. Using linking cubes, you will record the number of cubes needed to make each bridge collapse at various paper thicknesses.

Group Member Responsibilities

| Name | Minds On Card | Appointed Job |
| :--- | :--- | :--- |
|  | $\mathrm{y}=\mathrm{mx}+\mathrm{b}$ | Data Recorder <br> Records information from the <br> activity |
|  | Slope and Y-intercept | Materials Manager <br> Collects all the materials needed <br> Prepares paper and books |
|  | Standard Form | Model Designer <br> Creates each bridge model and <br> adds the load to the bridge <br> model |

### 3.11.3 London Bridge Is Falling Down... Instructions

## Preparation Instructions

1. Have the materials manager collect 30 linking cubes, a piece of masking tape, a plastic cup and 6 pieces of paper. (Your teacher may have already cut the paper for you by cutting a standard sheet of $8.5^{\prime \prime} \times 11^{\prime \prime}$ in half as shown below).

2. Fold $\mathbf{5}$ pieces of paper as shown below. These will be call you bridge planks.

3. Place a piece of masking take 2 cm from the edge of two textbooks. Make sure the spines of each book are facing outside as shown below.


### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

## Beam Bridge Instructions

4. Place the first bridge plank such that the ends of each plank touch the masking tape as shown below.

5. Next, place the plastic cup in the middle of the Beam Bridge.
6. Place a linking cube into the cup gently. Continue placing one linking cube at a time until the bridge collapses. The bridge must touch the desk for it to be considered a collapse.
7. Record this data on the data collection sheet provided.
8. Place another plank over top the first one creating a two layer plank bridge.

9. Place the empty cup in the middle of the bridge.
10. Repeat step 6-7
11. Repeat steps 8 - 10 for a 3, 4, and 5 layer plank beam bridge.

### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

## Arch Bridge Instructions

1. The next design is to create an arch bridge. Using the same textbooks and setup as the last bridge, place the unfolded piece of paper between the textbooks to form an arch as shown below.

2. Place one of the planks from the last activity on top of the arch making sure the ends of the plank coincide with the tape.
3. Place the empty cup in the middle of the plank.
4. Add linking cubes, one at a time until the bridge collapses.

5. Record this data on the data collection sheet provided.
6. Place another plank over top the first one creating a two layer plank bridge.
7. Place the empty cup in the middle of the bridge.
8. Repeat step 4-5
9. Repeat steps $6-8$ for a 3, 4, and 5 layer plank arch bridge.

### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

## London Bridge Is Falling Analysis

## Data Tables

1. Place the data from your investigation on the tables below

| BEAM BRIDGE |  |
| :--- | :--- |
| Number of Planks | Number of Cubes |
|  |  |
|  |  |
|  |  |
|  |  |
|  |  |


| ARCH BRIDGE |  |
| :--- | :--- |
| Number of Planks | Number of Cubes |
|  |  |
|  |  |
|  |  |
|  |  |

## Graphs:

2. Use this grid for the questions below.


### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

## Calculations:

3. What variable is the $x$-variable (independent) (Circle one): Number of Planks or Number of Cubes
4. What variable is the $y$-variable (dependent) (Circle one): Number of Planks or Number of Cubes
5. Create a scatter plot from the data of both bridges using a different colour for each data set. Label axes with appropriately.
6. Create lines of best fit for both sets of data using a different colour for each line.
7. From the Beam Bridge line of best fit, choose two points. Calculate the slope using these two points.
$\mathrm{m}=$ $\qquad$
8. Explain the significance of the slope in the context of this activity.
9. Using the slope and coordinates of one of the two points calculate the $y$-intercept by substituting into $\mathbf{y}=\mathbf{m x}+\mathbf{b}$ and solving for $\mathbf{b}$.
$\mathrm{b}=$ $\qquad$
10. Write the equation of the Beam Bridge.

### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

11. From the Arch Bridge line of best fit, choose two points. Calculate the slope from these two points.
$\mathrm{m}=$ $\qquad$
12. Explain the significance of the slope in the context of this activity.
13. Using the slope and coordinates of one of the two points calculate the $y$-intercept by substituting into $\mathbf{y}=\mathbf{m x + b}$ and solving for $\mathbf{b}$.
$\mathrm{b}=$ $\qquad$

### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

14. Write the equation of the Arch Bridge.
15. You want to be sure that a bridge can hold 100 cars at one time. If each car is represented by a linking cube, how many planks would your bridge need? Show work below.

| Beam Bridge | Arch Bridge |
| :--- | :--- |
|  |  |
|  |  |
|  |  |

16. You recently saw two bridges hold 250 "cars" at once. How many planks would be required to hold those cars for both bridges? Show work below.

| Beam Bridge | Arch Bridge |
| :--- | :--- |
|  |  |

### 3.11.3 London Bridge Is Falling Down...Instructions (Continued)

## Reflection:

17. What are the $x$-intercepts of both graphs? Interpret their significance in the context of this activity.
18. Which bridge presents a better design? Offer mathematical proof using data you collected and calculations you did.
19. One of your friends says the she constructed an amazing bridge but the plans were lost. The only thing left was the equation:

$$
5 x-3 y+15=0
$$

a. Graph this equation on the grid with your other two graphs
b. Using the graph, does this equation ever cross one of the other lines? What do these points mean in the context of this problem?
c. Based on the graph and the equation, is your friends bridge better, worse or the same as the Beam bridge? Offer mathematical proof.
d. Based on the graph and the equation, is your friends bridge better, worse or the same as the Arch bridge? Explain using mathematics.

### 3.11.4 London Bridge Is Falling Down... - Teacher Note

Below is a set of data based on this activity. You may choose to use this as an intervention for groups that do not get linear data.

| Number of Planks | Number of Cubes- <br> BEAM BRIDGE | Number of Cubes- <br> Arched Bridge |
| :---: | :---: | :---: |
| 1 | 2 | 3 |
| 2 | 6 | 9 |
| 3 | 11 | 16 |
| 4 | 17 | 23 |



Number of Planks

- The slope represents the number of cubes one can place per added plank.
- The y-intercept's meaning is much more abstract. In this context: the number of cubes needed to make the bridge collapse when no planks are used.
- The x-intercept has contextual meaning: the number of planks required when the bridge collapses on itself (i.e. this Beam Bridge has an x-intercept of 0.7 which means that a plank that is 0.7 thickness will collapse on its own weight)


## Unit 3 Equations of Lines Review

1. On a Cartesian coordinate system, plot and label the following points.
$A=(2,-1)$
$B=(4,10)$
$C=(1,7)$
$D=(2,-3)$
a) Draw the following lines: $A B \quad A C \quad B C \quad C D$
b) Calculate the slope for each line using a rate triangle:

Slope $(A B)=\quad$ Slope $(A C)=$

c) Calculate the following slopes algebraically. Verify with the graph.

Slope (BC)=
Slope (CD)=
2. Comparison of Slopes
a) If a line slants upward from left to right, it has a $\qquad$ slope.
b) If a line slants downward from left to right, it has a $\qquad$ slope.

## Unit 3 Equations of Lines Review (continued)

3. Draw two examples of lines with a positive slope and two examples of lines with a negative slope in the corresponding grids below.

## Lines With Positive Slopes



Lines With Negative Slopes

4. Circle the equations of the lines that are horizontal. Underline the equations of lines that are vertical.
a) $x=7$
b) $y=3$
c) $x=-3$
d) $y=5$
e) $y=3 x+6$
f) $y=-2$
5. Complete the sentences by filling in the blanks.

## Horizontal Lines

a) The equations of all horizontal lines are of the form $\qquad$ .
b) The slope of a horizontal line is $\qquad$ .
c) Horizontal lines do not cross the $\qquad$ axis.

## Vertical Lines

a) The equations of all vertical lines are of the form $\qquad$ .
b) The slope of a vertical line is $\qquad$ .
c) Vertical lines do not cross the $\qquad$ axis

## Unit 3 Equations of Lines Review (continued)

6. Write the equation of each line.

A: $\qquad$
C: $\qquad$
E: $\qquad$
F: $\qquad$

7. Graph and label the lines.

A: $x=3$
B: $y=-6$
C: $y=5$
D: $x=-6$

8. a) When the equation of a line has the form $y=m x+b$,
$m$ is the $\qquad$ of the line and
$b$ is the $\qquad$ .
b) State the slope and coordinates of the $y$-intercept for each.
i) $y=\frac{2}{5} x-4$
ii) $y=-3 x$
iii) $y=-2 x+5$
iv) $y=-3$
9. Write the equation of each line given:
a) slope 5 and y-intercept 3
b) $b=7 \quad m=-1 / 2$
c) slope of -2 and passing through $\mathrm{A}(0,4)$
d) slope parallel to $y=3 x+7$ with same $y$-intercept as $\mathrm{y}=8 \mathrm{x}-19$

## Unit 3 Equations of Lines Review (continued)

10. Find the equation of each line.
(a)

(b)

(a) $\qquad$
(b) $\qquad$
(c)

(d)

(c) $\qquad$
(d) $\qquad$
11. State two possible equations for each line.
a)


1) $\qquad$ 1) $\qquad$
2) $\qquad$ 2) $\qquad$
c) Justify your choices for $m$ and b:

## Unit 3 Equations of Lines Review (continued)

12. Draw rough sketches of the following lines showing the y intercept and slope triangle for each.


Answer the following questions based on the lines graphed below.
13. Which lines will have positive slopes?
14. Which lines will have negative slopes?
15. Fill in the table by listing the coordinates for the $x$-intercepts and $y$-intercepts.

| Line | $x-$ <br> intercepts | $\boldsymbol{y}$ - <br> intercepts |
| :---: | :---: | :---: |
| 1 |  |  |
| 2 |  | $(0,6)$ |
| 3 |  |  |
| 4 | $(-4,0)$ |  |



## Unit 3 Equations of Lines Review (continued)

16. How does knowing the $x$-intercept and $y$-intercept help you to graph a line?
17. Graph the following lines by finding the $x$ and $y$ intercepts.
a) $3 x-2 y-6=0$
b) $2 x-5 y-14=0$

18. Find the equation of the line given the point and slope.
a) $(2,1) ; m=3$
b) $(-3,4) ; m=3 / 4$
c) $(4,-5) ; m=-1$
d) $(5,0) ; m=-6$
19. Find the equation of the line joining the two given points.
а) $(2,1) ;(-3,4)$;
c) $(4,-5) ;(5,0)$;

## Unit 3 Equations of Lines Review (continued)

| Scenario | 1.Babysitting Earnings <br> A family pays the <br> babysitter $\$ 4.00 / \mathrm{hr}$, plus <br> a tip of $\$ 5.00$. | 2. Bank Account <br> Balance <br> A bank account is <br> opened with a balance <br> of $\$ 900$. Each week <br> $\$ 150$ is withdrawn from <br> the account. | 3. Car Rental Costs <br> Rent-A-Ride charges <br> a flat fee of \$55 plus <br> \$0.25/km to rent a <br> car. |
| :--- | :--- | :--- | :--- |
| Introduce Variables | Let $\mathrm{y}=$ |  |  |

